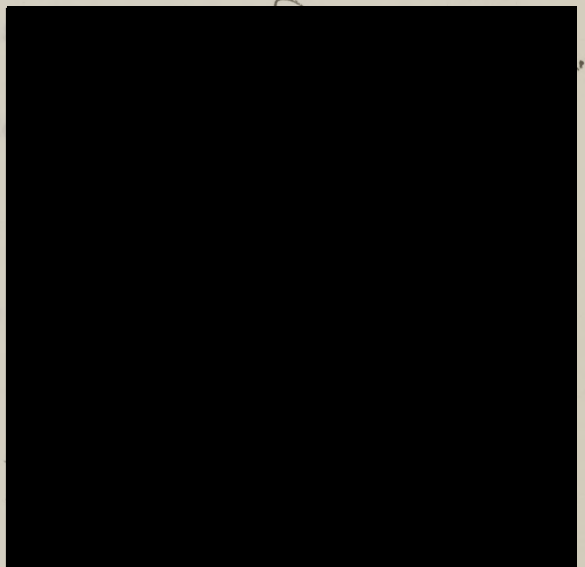


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NEUTRONS SCATTERED FROM IRON  
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The advice and encouragement of Dr. E. W. Little,  
Dr. is gratefully acknowledged. This dissertation is also  
expressed to all members of the Cockcroft-Walton group.  
Presented to the Faculty of APPROVED: Graduate School of  
The University of Texas

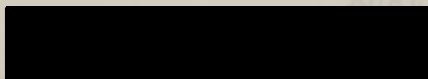
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The University of For the  
Austin, Texas  
DOCTOR OF  
June, 1953



By

Charles Patrick Cadenhead, B. S., M. A.  
APPROVED:

Austin, Texas



June 1953  
Dean of the Graduate School

DISTRIBUTION IN ENERGY AND ANGLE OF FAST  
NEUTRONS SCATTERED FROM IRON

PREFACE

The advice and encouragement of Dr. R. N. Little,  
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Presented to the Faculty of the Graduate School of  
The University of Texas in Partial Fulfillment

of the Requirements

C. P. C.

The University of For the Degree of  
Austin, Texas

DOCTOR OF PHILOSOPHY

June, 1953

By

Charles Patrick Cadenhead, B. S., M. A.

Austin, Texas

June 1953

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The advice and encouragement of Dr. R. N. Little, Jr. is gratefully acknowledged. Appreciation is also expressed to all members of the Cockroft Walton group. In particular, the help of J. E. Wills and H. R. Dvorak was invaluable.

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The University of Texas

Austin, Texas

June, 1953

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## CHAPTER I

or low resolutions. Activation cross sections for fast neutrons are, in INTRODUCTION low, and their energy dependence is seldom well known.

In the field of neutron physics progress has been slow because of the lack of a really good neutron detector. Many types of detectors have been used with various results. The ideal detector would combine high efficiency with either good energy resolution or detection of all energies with equal efficiency. So far this ideal detector has not been realized. The two primary principles which have been used in detection are the observation of the recoil of nuclei (principally hydrogen and helium) from a collision with a neutron and the activation of nuclei by neutron capture with later emission of particles which can be detected. The observation of proton recoils either in a photographic emulsion or in a cloud chamber gives the best results on measurements of energy of the neutrons. Both of these methods suffer from the long times involved in obtaining the desired information, not only from the exposure-to-radiation time, but also because of the generally much longer time required to extract the results from the films used. Ionization chambers and other types of recoil counters have also been used, but they too suffer from very low efficiencies

## CHAPTER II

or low resolutions. Activation cross sections for fast neutrons are, in general, quite low, and their energy dependence is seldom well known.

There are two processes through which neutrons may lose energy in passing through matter. The first of these is the so-called elastic scattering and the second is inelastic scattering. These two subdivisions of the order of 10 to 50% for the detection of neutrons. Efficiencies of this order of magnitude have made feasible the performance of experiments which could be accounted for by assuming the conservation of momentum of the two particles, then the scattering is called elastic. If the energy loss is more than can be accounted for in this way, the scattering is called inelastic.

The present experiment is an attempt to analyze the energy distribution of the neutrons scattered at a particular angle when a beam of monoenergetic neutrons is incident on the scatterer and hence to measure:

(1) differential angular elastic scattering cross sections, (2) differential angular inelastic scattering cross sections and (3) analyze the energy distribution of the scattered neutrons.

techniques of optical diffraction theory. The angular

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1. Feld, Feshbach, Goldberger, Goldstein, Weiskopf, "Final Report of the Fast Neutron Data Project", NYO-636, U. S. Atomic Energy Commission.

---

distribution of the scattered neutrons with this treatment shows a strong maximum in the forward direction and decreases to a more or less constant value in the



## CHAPTER II

back direction where the major effect is that of reflection scattering. SCATTERING PROCESSES

There are two processes through which neutrons may lose energy in passing through matter. The first of these is the so-called elastic scattering and the second is inelastic scattering. These two subdivisions are made on the basis of the energy losses involved. If the energy loss in a collision is exactly that which can be accounted for by assuming the conservation of momentum of the two particles, then the scattering is called elastic. If the energy loss is more than can be accounted for in this way, the scattering is called inelastic.

Elastic scattering can be subdivided into two groups, potential elastic scattering and resonant or capture elastic scattering. The behavior of the potential elastic scattering can be calculated using the techniques of optical diffraction theory.<sup>1</sup> The angular

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1. Feld, Feshbach, Goldberger, Goldstein, Weisskopf, "Final Report of the Fast Neutron Data Project", NYO-636, U. S. Atomic Energy Commission.

---

distribution of the scattered neutrons with this treatment shows a strong maximum in the forward direction and decreases to a more or less constant value in the

back direction where the major effect is that of reflection scattering. Capture elastic scattering, on the other hand is actually a special case of inelastic scattering, in that the neutron actually "enters" the nucleus but is re-emitted from the nucleus with the same energy it originally possessed, except for the energy of the recoil nucleus. This type of scattering may be isotropic under certain conditions which will be discussed under inelastic scattering.

Inelastic scattering occurs when a neutron enters the nucleus and is re-emitted with a loss of energy leaving the residual nucleus in a state of excitation. The residual nucleus generally decays to the ground, or original level, by subsequent emission of one or more gamma rays. Inelastic scattering is the main source of energy loss for high energy neutrons and heavy nuclei, while elastic scattering is more effective for low energy neutrons and light nuclei.

One of the better summaries to date of the theoretical work on scattering cross sections to date has been made by Feld, et al.<sup>2</sup> Their work has served as a

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2. Feld, Feshbach, Goldberger, Goldstein, Weisskopf, ibid.

---

guide for some of the following remarks.



For calculation and discussion purposes, it is convenient to divide inelastic scattering processes into three classes, distinguished by the possibility of applying statistical theory to the problem, that is, whether there are a large number of excitation levels available or not. The characteristics of the three classes are:

I. A statistical approach is not valid for the energy losses corresponding to the energies of the compound or the residual nucleus.

II. A statistical approach is valid for the compound nucleus but is not valid for the residual nucleus.

III. A statistical approach is valid for both the compound and the residual nucleus.

In terms of the masses of the nuclei in the energy range used, nuclei with masses less than approximately 20 belong to class I, nuclei with masses between 20 and 100 as well as the heavy "magic" nuclei belong to class II, and the heavy nuclei belong to class III. Iron has a mass of 56 and the 2.8 mev. of the incident neutron energy plus the binding energy of the neutron give a high enough excitation level so that many levels should be excited in the compound nucleus, while only discrete levels have been observed in the residual nucleus. One further result can be obtained from

nucleus.<sup>3,4</sup> Nuclei of class II should yield valuable

---

3. Day, R. B., Phy. Rev. 89, 908 (1953).

4. Elliot, L. G. and Deutsch, M., Phy. Rev. 63, 321 (1943).

---

The information on angular distribution of scattered neutrons, coupled with information obtained in other ways, should lead to unambiguous assignments of spin and parity to the levels of nuclei. The inelastically scattered neutrons will emerge in groups with energy losses corresponding to the energies of the various excited levels and with numbers proportional to the total cross section for the excitation of each level.

It is also of great interest to observe the angular distribution of the neutrons from each of the excited levels. According to Feld, et al.<sup>5</sup>, the angular

---

5. Feld, Feshbach, Goldberger, Goldstein, Weisskopf, op cit.

---

distribution (for class II nuclei) should be an even function of  $\cos \theta$  where  $\theta$  is the angle of emission referred to the direction of the incident neutron. This is a consequence of the assumption that the statistical model of the nucleus is valid for the compound nucleus and failure of this symmetry would indicate that the statistical model is not valid for the compound nucleus. One further result can be obtained from



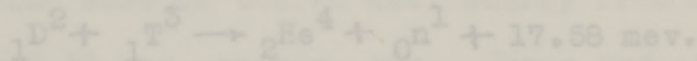
## CHAPTER III

the angular distribution. The highest power of  $\cos \theta$  that can appear in the angular distribution is determined by the angular momentum quantum number of either

the incident or the emitted neutron with respect to the nucleus. The information on angular distribution of scattered neutrons, coupled with information obtained

in other ways, should lead to unambiguous assignments of spin and parity to the levels of nuclei.

The  $D(d,n)$  reaction, symbolically



yields neutrons of approximately 14 mev. The first of these reactions was used in the present experiment.

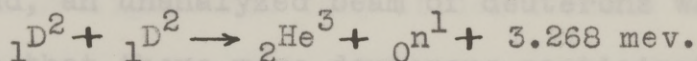
The 100 kv. linear accelerator in the University of Texas Physics Department was used to accelerate deuterium ions to energies of 100,000 volts. These deuterium ions were then allowed to strike the bottom of a thin copper sphere where some of the ions were occluded into the copper and other of the ions reacted with the occluded ions, whereupon the  $D(d,n)$  reaction took place yielding neutrons of approximately 2.6 mev. in the forward direction. This type of target was used instead of a specially prepared target because of the ease of preparation. The total number of neutrons produced was of the order of  $10^6$  per second at an occluded beam current of 500 microamperes.

## CHAPTER III

### APPARATUS

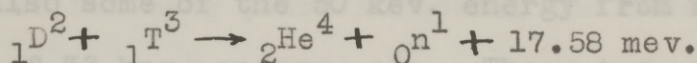
There are two nuclear reactions which will yield large numbers of neutrons at low bombarding energy.

The D(d,n) reaction, symbolically



yields neutrons of energy approximately 2.5 mev. The

T(d,n) reaction, symbolically



yields neutrons of approximately 14 mev. The first of these reactions was used in the present experiment.

The 100 kv. linear accelerator in the University of Texas Physics Department was used to accelerate deuterium ions to energies of 100,000 volts. These deuterium ions were then allowed to strike the bottom of a thin copper sphere where some of the ions were occluded into the copper and other of the ions reacted with the occluded ions, whereupon the D(d,n) reaction took place yielding neutrons of approximately 2.8 mev. in the forward direction. This type of target was used instead of a specially prepared target because of the ease of preparation. The total number of neutrons produced was of the order of  $10^6$  per second at an unanalyzed beam current of 500 microamperes.



The emitted neutrons were not completely monoenergetic because of three factors: first, a "thick" target is the source of the neutrons. Since the energy of the neutrons is a function of the bombarding energy, there will be some neutrons of slightly lower energy. Second, an unanalyzed beam of deuterons was used, which means that there were deuterons participating in the reaction which had not only 100 kev. from atomic ions but also some of the 50 kev. energy from molecular ions, some of 33 kev. energy, etc. These two effects on the neutron energy are comparatively small (the difference between half-maximum points of the neutron energy peak having been measured to be 0.3 mev.<sup>6</sup>) because of the

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6. Brundage, R. S., "Total Cross Section of Aluminum for D(d,n) Neutrons", unpublished M. A. Thesis, University of Texas, June 1952.

---

rapidly increasing yield of the reaction as the energy of the ions is increased. The third factor in the spread of the energy of the neutrons is the variation of the energy of neutrons as a function of the angle of neutron emission with respect to the incident deuteron beam. This latter effect was minimized by taking advantage of the symmetry of the energy variation about the axis of the deuteron beam by using circular ring scatterers. It was also desirable to allow some small

variations of neutron energy in order to take advantage of the much larger fluxes of neutrons available when an unanalyzed beam and thick targets were used.

From the early days of nuclear physics it was realized that nuclear particles would produce small amounts of light when they struck certain fluorescent substances. While this phenomenon was used to a large extent in early experiments, it became of small practical use for many years following the development of counter tubes. In recent years the development of the electron multiplier type of tube, which can give tremendous amplification of the current pulses produced by photoelectrons ejected from the cathode of the tube by light quanta, has changed the scintillation method from a state of mere interest to one of great usefulness in every nuclear physics laboratory. The electron photomultiplier has been the means of counting neutrons at rates and efficiencies heretofore unheard of. The first scintillation counters consisted of screens covered with a thin layer of zinc sulfide with the scintillation light pulses from alpha rays being observed visually. This is indeed a far cry from the present scintillation counter systems which can differentiate between pulses coming  $10^{-8}$  sec. apart and can measure the total amount of light from each pulse quite



accurately.

In the last few years several experimenters<sup>7,8,9</sup>

- 
7. Hofstadter, R., Nucleonics 6, No. 5, 70 (1950).
  8. Kallmann, H. and Furst, M., Phy. Rev. 79, 857 (1950).
  9. Jordan, W. H. and Bell, P. R., Nucleonics 5, No. 4, 30 (1949).
- 

have measured the efficiencies of various substances as scintillators. Certain types of scintillators operate best for counting one type of particle while others operate better for counting other types of particles. In particular, for counting neutrons it is desirable, in most cases, to use some hydrogenous material for the bulk, at least, of the scintillator, although it may be necessary to put small amounts of other material in the detector to produce a higher light production per scintillation. The hydrogenous material is desirable because of the fairly high cross section of protons for neutrons, and because the recoil protons can receive the most energy from the neutrons per collision.

Pure liquids make very poor scintillating material. However, if solutions are used, then it is possible to get strong fluorescence which has the spectral characteristics of the solute molecules.<sup>10</sup> For many purposes

- 
10. Falk, C. E. and Poss, H. L., Am. Jour. Phy. 20, 429 (1952).
-

liquid scintillators are very useful, since one of the big problems of solid scintillators was the production of good crystals which were as large as desired. The use of liquid scintillators allows the counter size to be as large as desired within the limits of self-absorption and other effects. Also the production of various shapes with liquids is considerably easier than with some of the solid crystals which are used.

The scintillator used in this experiment was of the liquid type, consisting of a solution of five grams of terphenyl per liter of m-xylene.<sup>11,12</sup> The terphenyl

- 
11. Dvorak, H. R., "Total Cross Sections of Bromine, Chlorine, Sodium and Titanium", Ph. D. Dissertation, May, 1953 (to be published).
  12. Schaeffer, N. M., "Scattering of D(d,n) Neutrons from Plane Slabs", Ph. D. Dissertation, May, 1953 (unpublished).
- 

furnishes the scintillation material while the xylene furnishes the hydrogenous carrier. After mixing the solution, it was placed in a glass holder which was then sealed with a teflon stopper. The glass and the teflon are desirable because of their inertness with respect to the solution. If materials are used to contain the solution which will react with or dissolve in the solutions, the liquid soon becomes contaminated with a consequent loss of efficiency and will eventually



have to be replaced. The glass cell was a cylinder 5.1 cm. in diameter and 5 cm. long. One end was concave to match the curvature of the 5819 photomultiplier and the other end was correspondingly convex.

After the glass container had been sealed, it was optically coupled to the 5819 photomultiplier tube with a Dow Corning type 200 fluid. The glass cell was then wrapped with crinkled aluminum foil for better light collection at the photocathode, and the cell and tube were wrapped with black photographic tape to prevent extraneous light from reaching the photocathode and causing spurious pulses. A 2 mm. thick lead shield was then placed over the scintillator head to attenuate any x-rays coming from the accelerator. Figure 1 is a block diagram of the circuitry involved.

Since the current multiplication of the photomultiplier tube is extremely high, it is necessary to keep the voltage on the tube as stable as possible. The high voltage supply for the electron multiplier tube followed the design of the Oak Ridge Dwg. Q-1144-1 power supply. The voltage applied to the photomultiplier tube was checked frequently with a Rubicon potentiometer arrangement and was found to be extremely stable after the resistors and the voltage dividers were allowed to reach stable temperature. If the

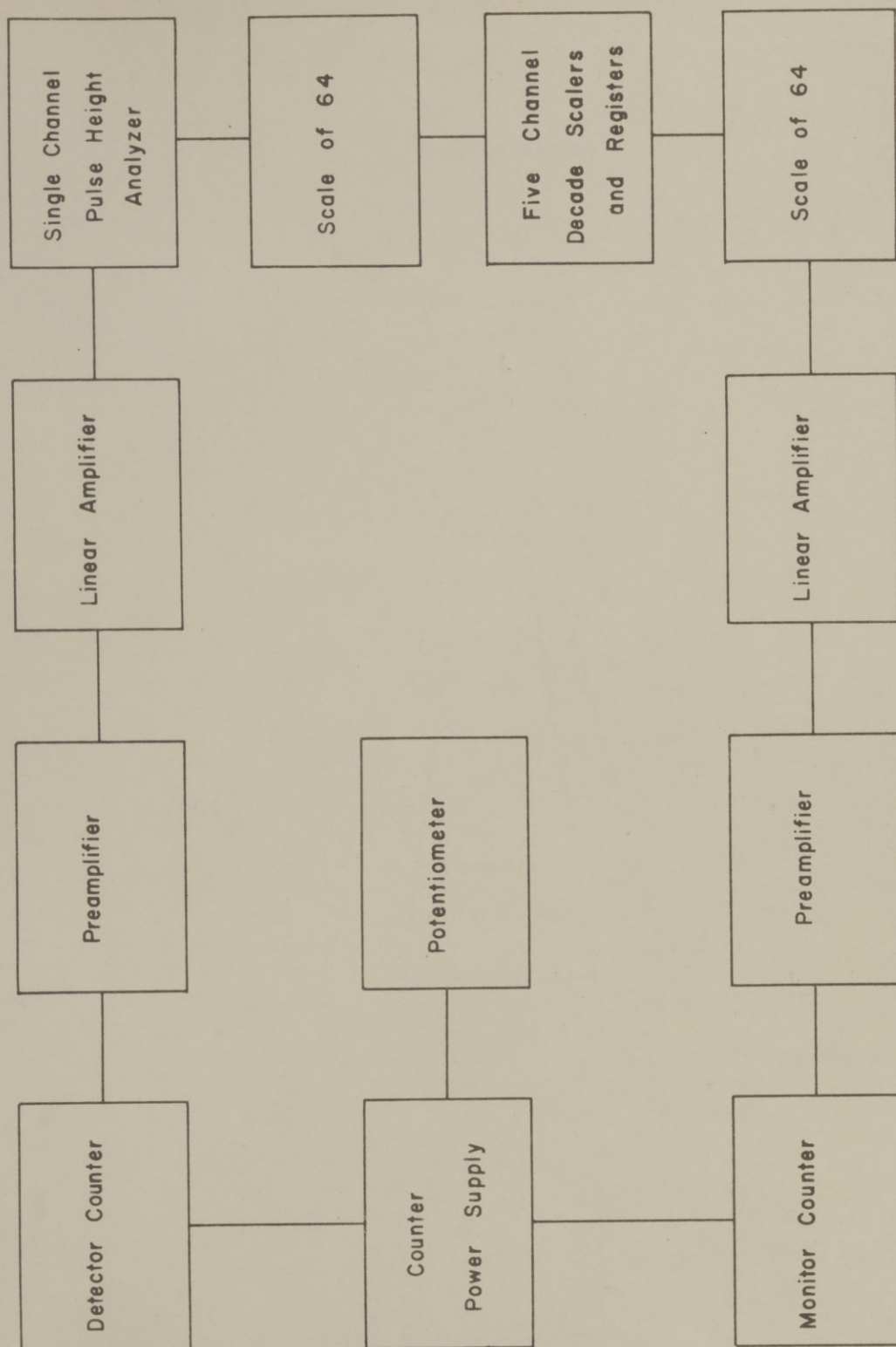


FIGURE 1. BLOCK DIAGRAM OF EQUIPMENT



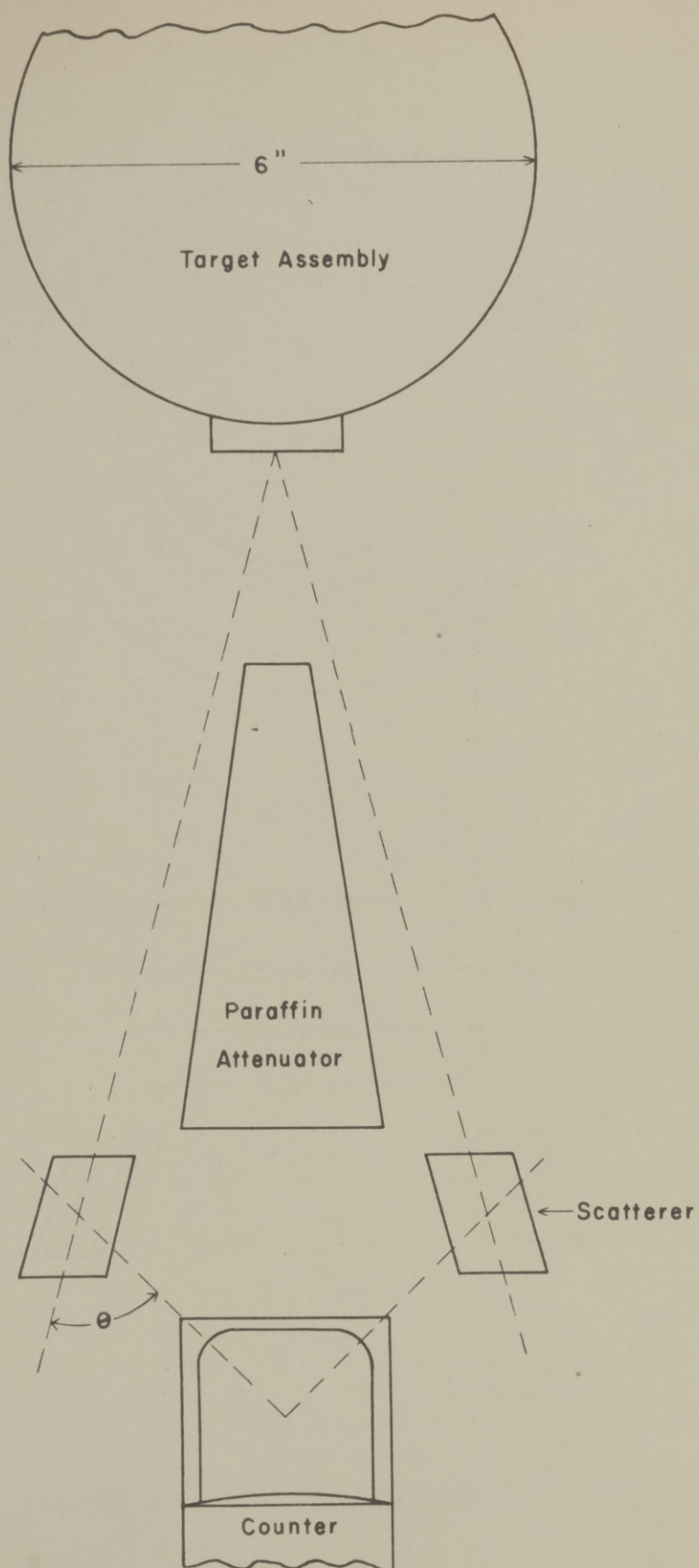


FIGURE 2. GEOMETRY OF EXPERIMENT

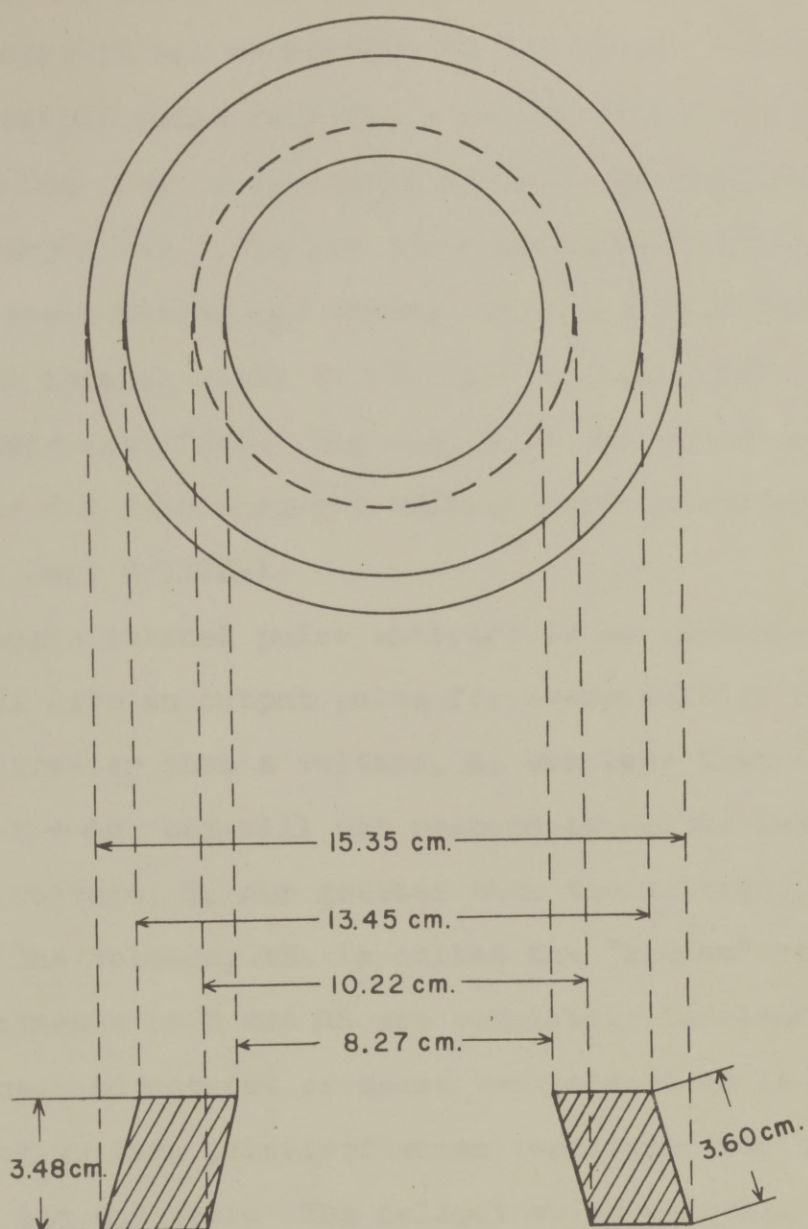


FIGURE 3. IRON SCATTERER



voltage was found to be different by more than a tenth of a per cent it was readjusted to the proper value.

The output pulse from the anode of the photomultiplier was fed into an impedance matching cathode follower preamplifier. The low impedance output pulse from the preamplifier was carried by a six foot length of RG-71/U coaxial cable to the input of the Atomic 204-B linear amplifier. The output of the linear amplifier was fed into a single channel pulse analyzer, Oak Ridge Dwg. Q-1192-1. Model 101-M scaler. The output

A single channel pulse analyzer is an instrument which will give an output pulse for every voltage pulse which is greater than a voltage,  $E$ , but less than a voltage,  $E + \Delta E$ ; but will not respond to pulses less than the voltage,  $E$ , nor greater than the voltage,  $E + \Delta E$ . The voltage,  $\Delta E$ , is called the "window" width. The adjustments of  $E$  and  $\Delta E$  are completely independent operations. Adjustment of these two parameters is made by feeding voltage pulses of known amplitude into the input of the analyzer. The helipot which controls  $E$  is calibrated by observing the minimum setting at which pulses will be counted. The helipot which controls  $\Delta E$  is calibrated by observing the difference between the minimum setting of  $E$  at which pulses will be counted and the maximum setting of  $E$  at which pulses will be

## CHAPTER IV

counted. The actual choice of a  $\Delta E$  for a particular experiment will be determined by a compromise between the resolution desired and the time required to obtain a reasonable number of counts. If  $\Delta E$  is made too large, then details of the spectrum may be lost. On the other hand, if  $\Delta E$  is made too small, the length of time required to obtain small statistical variations is prohibitive.

The output pulses from the single channel analyzer are fed into an Atomic Model 101-M scaler. The output of the scaler is in turn fed into a Berkeley Model 3501 five channel decade counter and register.

The neutron flux was monitored at all times by a similar counter system with the exception that all pulses above a certain height were recorded. The discriminator of the Atomic amplifier was used instead of the single channel analyzer for setting the minimum height pulses counted. The switches of the scalers for the detector and for the monitor were mechanically ganged together so that they could be operated simultaneously. A Standard electric timer was used to measure the time of each run.



## CHAPTER IV

linear amplifier and the pulse height analyzer should be allowed to warm up

### PROCEDURE

The first step in the operation of the single-channel differential pulse height analyzer is to calibrate the width of the counting channel as a function of the pulse height control. Pulses of constant height and frequency are fed into the input of the analyzer. The "discriminator output" jack of one of the scalers is a convenient source of such pulses when the scaler is operated on the 60 cycle test position. The analyzer is set on the differential position and the channel width control ( $\Delta E$ ) is set for the maximum width. The discriminator (E) control is turned slowly until pulses are counted. The maximum position of E and the minimum position of E at which pulses are still counted are noted. Since the  $\Delta E$  dial is fairly linear, the dial can then be roughly set to the desired width. The adjustment of the  $\Delta E$  control is then completed by carefully noting the points at which the counting rate falls off to one half the maximum value on each side and adjusting the  $\Delta E$  control until it corresponds to the desired width. The analyzer is now ready to be reconnected to the output of the linear amplifier and put into operation. It is worth noting that the

linear amplifier and the pulse height analyzer should be allowed to warm up for several hours before being put into operation. Since the voltages in the scalers are not as critical, a few minutes of warm-up time suffice for them.

Voltage is applied to the 5819 photomultiplier tube, and the voltage divider supplying the various voltages to this tube is allowed to reach an equilibrium condition, after which the voltage is measured by means of the Rubicon potentiometer. Background counting rates are measured with the high voltage of the accelerator on but with no beam current.

Two different types of runs are made. First, the counter is placed in position and the counting rate as a function of the discriminator setting,  $E$ , (called hereafter the "discriminator spectrum") is obtained. All runs are made by first taking the counting rate with the scatterer in, then removing the scatterer and again obtaining the counting rate. The difference between these two intensities (called  $\Delta I$ ), all other conditions being constant, is due to the presence of the scatterer. After the discriminator spectrum has been obtained, a decision must be made as to where the discriminator should be set in order to obtain the desired angular scattering cross sections. Then the second



## CHAPTER V

type of run is made, in which the discriminator is fixed at one or more values, and the counter position is varied so as to vary the average angle of scattering. All counting rates were divided by the counting rate obtained on a similar scintillation counter (the monitor) which was placed a distance of 55 cm. from the source of neutrons. The counting rates are then given as counts/monitor count which nullifies the effect of variations in the number of neutrons from the target for different "runs". The count switches of the two counters were operated at the same time, thus preventing small errors in time measurement from affecting the final results.

- 
14. Kruger, Shoup and Slatten, *Exp. Rev.* **22**, 578 (1937).
  15. Bonner, T. W., *Phys. Rev.* **52**, 552 (1937).
  16. Coon, J. H. and Barschall, H. E., *Phys. Rev.* **70**, 592 (1946).
  17. Barschall, H. E. and Treiman, S. F., *Phys. Rev.* **73**, 1819 (1949).
- 

system. Under these conditions, the fraction of protons scattered into a segment of a spherical surface defined by the angles  $\theta$  and  $\theta + d\theta$  (where  $\theta$  is the angle between the incident neutron and the scattered proton) is

## CHAPTER V

### ANALYSIS OF DATA

Baldinger, Huber and Staub<sup>13</sup> first pointed out

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13. Baldinger, Huber and Staub, Helvetia Physica Acta 11, 245 (1938).
- 

that the distribution in energy of recoil protons from fast neutrons bears a very simple relationship to the distribution in energy of the neutrons, and that this relationship can be used to distinguish between elastically and inelastically scattered neutrons. The scattering of fast neutrons by protons has been shown<sup>14,15,16,17</sup> to be isotropic in the center of mass

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14. Kruger, Shoupp and Slattman, Phy. Rev. 52, 678 (1937).  
15. Bonner, T. W., Phy. Rev. 52, 685 (1937).  
16. Coon, J. H. and Barschall, H. H., Phy. Rev. 70, 592 (1946).  
17. Barschall, H. H. and Taschek, R. F., Phy. Rev. 75, 1819 (1949).
- 

system. Under these conditions, the fraction  $dN$  of protons scattered into a segment of a spherical surface defined by the angles  $\phi$  and  $\phi + d\phi$  (where  $\phi$  is the angle between the incident neutron and the scattered proton) is



$$dN = \frac{2\pi N_0 \sin\phi \, d\phi}{4\pi} = \frac{N_0 \sin\phi \, d\phi}{2}$$

where  $N_0$  is the total number of protons scattered.

When transformed to the laboratory system, since  $\phi = 2\theta$  where  $\theta$  is the corresponding angle in the laboratory system, this expression becomes

$$dN = N_0 \sin 2\theta \, d\theta = 2N_0 \sin\theta \cos\theta \, d\theta.$$

Now the energy of the recoil proton in the laboratory system  $E_p$  is

$$E_p = E_n \cos^2\theta$$

where  $E_n$  is the energy of the incident neutron. Hence

$$dE_p = -2E_n \cos\theta \sin\theta \, d\theta$$

and

$$\frac{dN_p}{dE_p} = \frac{2N_0 \sin\theta \cos\theta \, d\theta}{-2E_n \cos\theta \sin\theta \, d\theta} = -\frac{N_0}{E_n}.$$

Thus the recoil protons from a monoenergetic beam of neutrons are evenly distributed in energy from zero energy up to the energy of the neutrons. Figure 4A illustrates the distribution in energy of recoil protons from monoenergetic neutrons. Now if there is a second group of monoenergetic lower energy neutrons also present, the distribution would be of the nature as shown in Figure 4B. Since it is impossible experimentally to obtain completely monoenergetic neutrons,

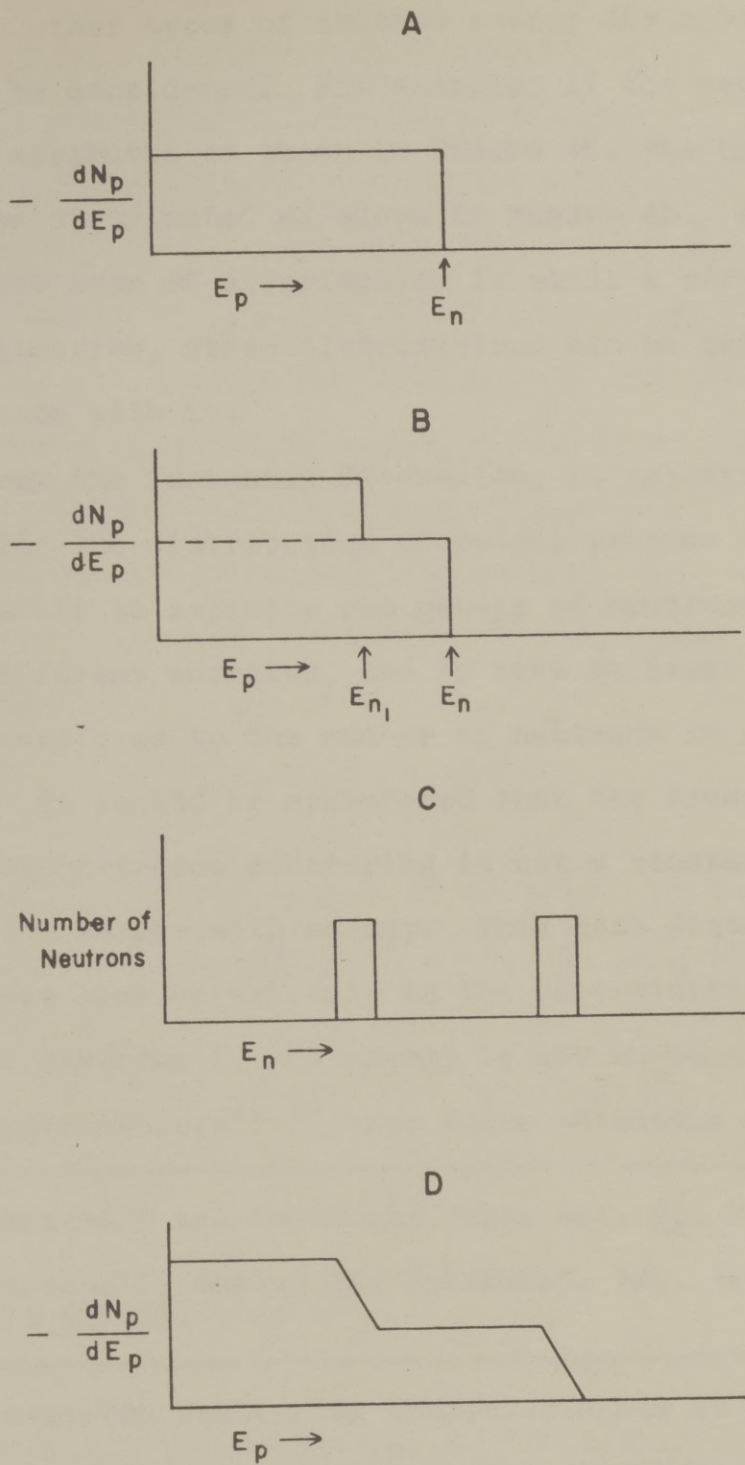


FIGURE 4. IDEALIZED PROTON RECOIL DISTRIBUTIONS



certain other types of neutron energy distribution should be considered. For example, if the neutrons were distributed as shown in Figure 4C, the protons would be distributed as shown in Figure 4D. Although this last type of distribution is still a very idealized situation, other distributions can be inferred by comparison with it.

From the foregoing discussion, it appears that by observing the distribution of recoil protons it should be possible to separate out groups of neutrons which have different energies, and to make at least intelligent guesses as to the number of neutrons in each group. It should be remembered that the cross section for neutron-proton scattering is not a constant quantity, but varies with energy. This last factor may introduce some uncertainty in the determination of numbers of neutrons if the energy is not known exactly.

Experimenters<sup>18,19</sup> have taken advantage of the

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18. Barschall and Ladenburg, *Phy. Rev.* 61, 129 (1942).

19. Barschall, Manley and Weisskopf, *Phy. Rev.* 72, 875 (1947).

---

neutron-proton scattering characteristics by using ionization chambers to examine neutron spectra. The disadvantage is that the efficiency of ionization chambers is so low that the time required to obtain reliable data is quite long. On the other hand, the density of

nuclei in a liquid or solid scintillation counter is much greater, and hence the efficiency is considerably higher. This higher efficiency makes experiments feasible which were impractical with ionization chambers.

Figure 2 shows the geometry used with the iron scatterer. A ring type of geometry was chosen to have the maximum number of scattered neutrons for a given scatterer thickness and given geometrical latitude on the angle of scattering for the neutrons.

Differential angular scattering cross section may be defined as

$$\frac{d\sigma(\theta)}{d\omega} = \frac{N(\theta)}{n_1 N_s}$$

where  $N(\theta)$  is the number of neutrons per steradian scattered at an angle,  $\theta$ ,  $n_1$  is the number of scattering centers per square centimeter, and  $N_s$  is the number of neutrons incident on the scatterer. In order to use this formula, it is necessary to express it in terms of the parameters of the experiment. Now

$$N(\theta) = \frac{\delta I R^2}{c A_d}$$

where:  $c$  = the efficiency of the counter

$\delta I$  = the number of counts from scattered neutrons

$R$  = the distance from the scatterer to the detector



where:  $A_d$  = the area of the detector.

$N_s$  should be the average number of neutrons falling on the scatterer. Since the scatterer is not infinitely thin, a correction must be made for the neutrons which are scattered out of the neutron beam. The number,  $N$ , of neutrons at a depth,  $x$ , of the scatterer is given by  $N = N_0 e^{-n\sigma_t x}$  where  $N_0$  is the number of neutrons incident on the surface of the scatterer,  $n$  is the number of scattering centers/cm.<sup>3</sup> and  $\sigma_t$  is the total cross section for the scattering material. Thus the average number of neutrons in the scatter,  $N_s$ , is given by

$$\begin{aligned} N_s &= \bar{N} = \frac{1}{a} \int_0^a N_0 e^{-n\sigma_t x} dx \\ &= \frac{N_0}{n\sigma_t a} (1 - e^{-n\sigma_t a}) \end{aligned}$$

where  $a$  is the total thickness of the scatterer or, since  $na = n_1$

$$N_s = \frac{N_0}{n_1 \sigma_t} (1 - e^{-n\sigma_t a}).$$

Expressing  $N_0$  in terms of the counting rate of the detector gives

$$N_0 = \frac{f I_0 A_s d_4^2}{c A_d r_1^2}$$

21. Leonard, "The Differential Angular Scattering of Neutrons by Aluminum and Copper", Ph. D. Dissertation, University of Texas, May, 1953 (to be published).

where:  $A_s$  = the area of the scatterer subtended at  
simplified to the target

$d_4$  = the distance from the target to the detector

$r_1$  = the distance from the target to the scatterer

$I_0$  = the counting rate of the detector due to the direct beam of neutrons from the target

$f$  = a numerical factor to account for the difference in the intensity of the beam of neutrons at the scatterer angle and the intensity of the beam in the forward direction. This difference occurs because of the angular asymmetry of the neutron distribution from the target.

The formula for differential angular scattering cross section then becomes<sup>20,21</sup>

$$\frac{d\sigma(\theta)}{d\omega} = \frac{\sigma_t R^2 r_1^2 \delta I}{f A_s d_4^2 (1 - e^{-n\sigma_t a})}$$

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20. Barschall and Ladenburg, op cit.

21. Leonard, B. P., "The Differential Angular Scattering of Neutrons from Aluminum and Copper", Ph. D. Dissertation, University of Texas, May, 1953 (to be published).

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For a given position of the scatterer, this can be simplified to

$$\frac{d\sigma(\theta)}{d\omega} = K \frac{R^2 \delta I}{d_4^2 I_0}$$

The values of K used in the calculations are listed in the data tables.

The procedure in measuring inelastic cross section is first to measure the differential angular scattering with a high value of the discriminator voltage, E, where the dominant factor in the counting rate is the elastically scattered neutrons, and then to measure the differential angular scattering at a low value of the discriminator voltage, E, where the counting rate is due to both elastically scattered and inelastically scattered neutrons. The difference in cross sections should be corrected for the change in neutron-proton cross section since the lower energy neutrons have a higher probability of collision with protons.

Figure 5 shows the discriminator spectrum obtained when the counter is exposed to the direct beam of neutrons from the target. The discriminator voltages are expressed in terms of divisions of the E dial. If conversion to voltage is desired, 1500 divisions of E equals 80 volts. This discriminator spectrum corre-

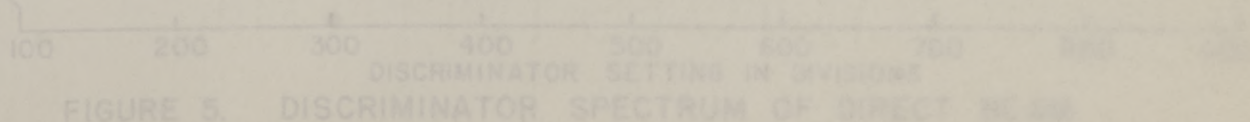


FIGURE 5. DISCRIMINATOR SPECTRUM OF DIRECT BEAM

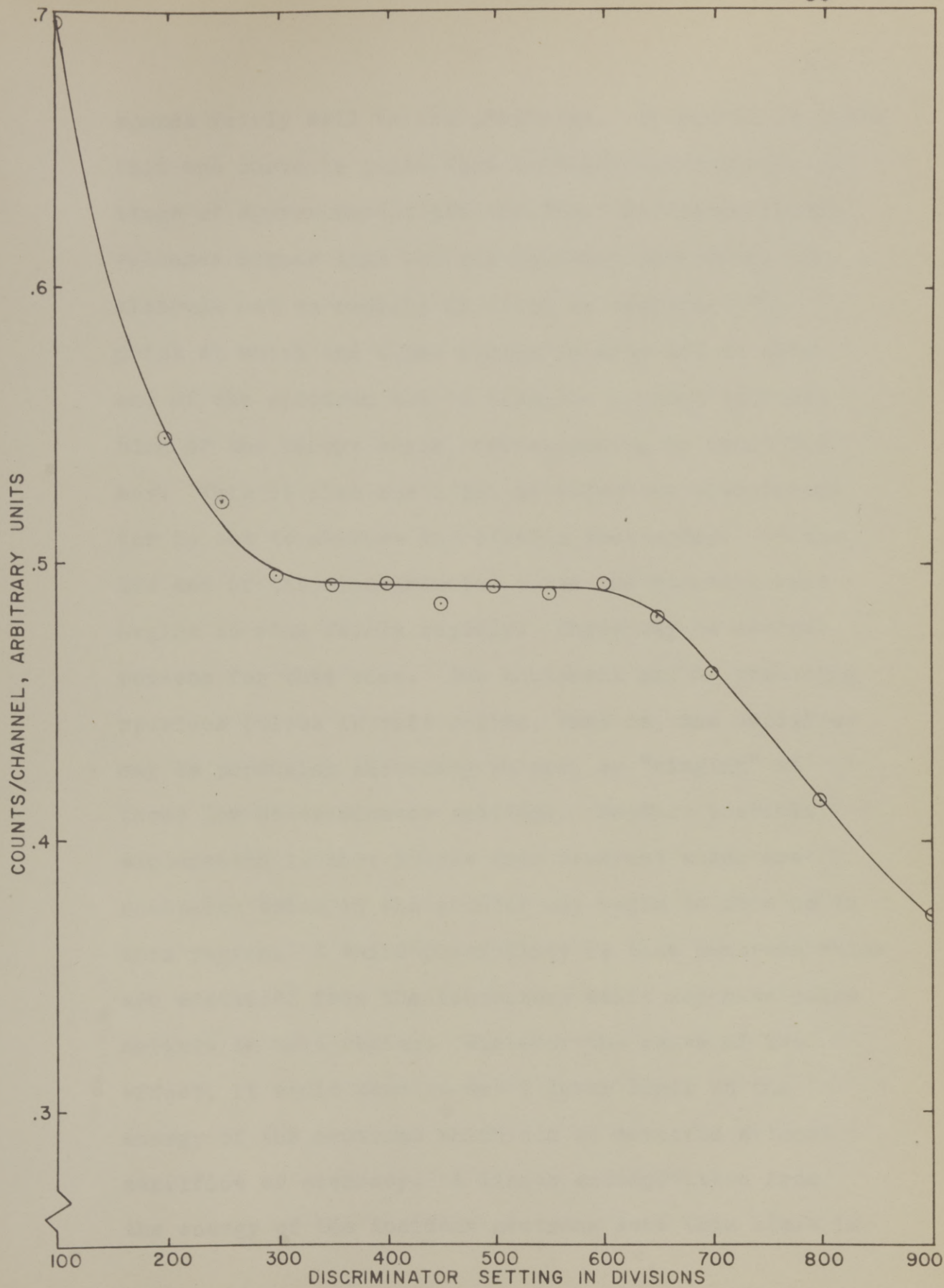


FIGURE 5. DISCRIMINATOR SPECTRUM OF DIRECT BEAM



sponds fairly well to the predicted. It should be noted that the curve is quite flat between discriminator settings of approximately 650 and 250. At discriminator voltages higher than 650 the counting rate drops off, although not as rapidly as might be desired. The point at which the curve begins to drop off at this end of the spectrum can be taken as a rough calibration of the energy scale, corresponding to about 2.8 mev. This is also the point at which the discriminator is set to measure the elastic scattering. On the low end of the discriminator curve the counting rate begins to rise fairly rapidly. There may be several reasons for this rise. The equipment may be producing spurious pulses in this region, that is, the amplifier may be producing secondary pulses, or "ringing" at these low discriminator settings. Another possible explanation is that pulses from neutrons which are scattered twice in the counter may begin to show up in this region. A third possibility is that neutrons which are scattered from the laboratory walls may have pulse heights in this region. Whatever the cause of the effect, it would seem to set a lower limit on the energy of the neutrons which can be detected without sacrifice of accuracy. A linear extrapolation from the energy of the incident neutrons sets this limit in

the region between 0.5 and 1.0 mev. It may be possible to lower this limit slightly, but since the amplifier is non-linear for pulses which are larger than about 1050 divisions on the discriminator, increasing the amplifier gain would tend to destroy the accuracy on the high end of the discriminator.

Figure 6 and Figure 7 show the discriminator spectrum of the scattered neutrons. Figure 6 shows data obtained without the use of an attenuator, and Figure 7 shows data taken with an attenuator. The general shapes of the curves are the same, although the data taken with an attenuator seems to show more detail than the data taken without an attenuator. This can be accounted for by the higher statistical accuracy obtained with the attenuator. There is a very definite break in the curve at a discriminator setting of approximately 300. It is believed that the variations from a smooth curve are actually due to the appearance of the inelastically scattered neutrons from the different levels of the residual iron nucleus. The appearance of these breaks mark places which should be investigated by the angular scattering method. These breaks, then, are the deciding factor in setting the discriminator bias for measuring inelastic scattering.

For each inelastically scattered neutron there



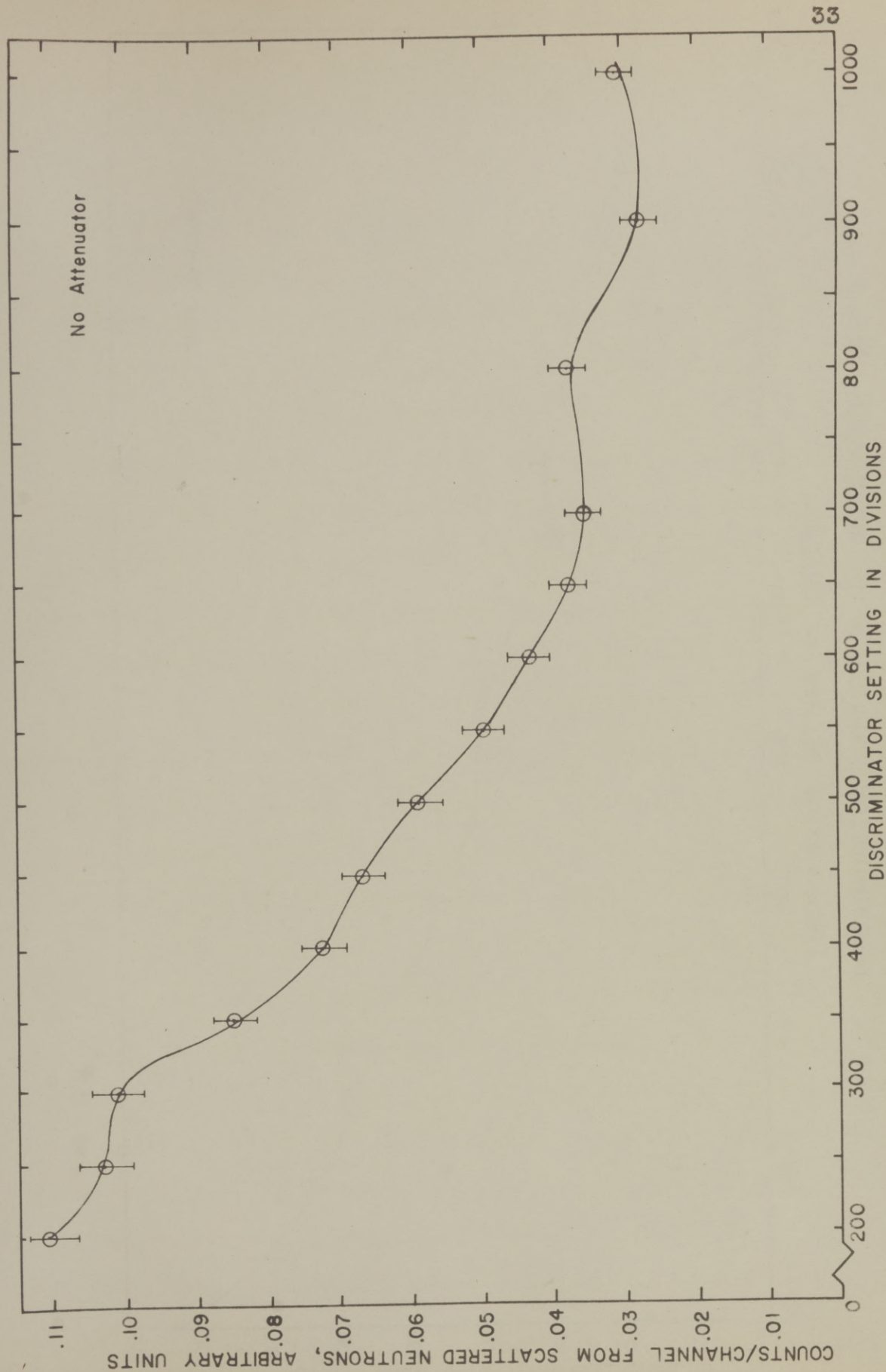


FIGURE 6. DISCRIMINATOR SPECTRUM OF SCATTERED NEUTRONS

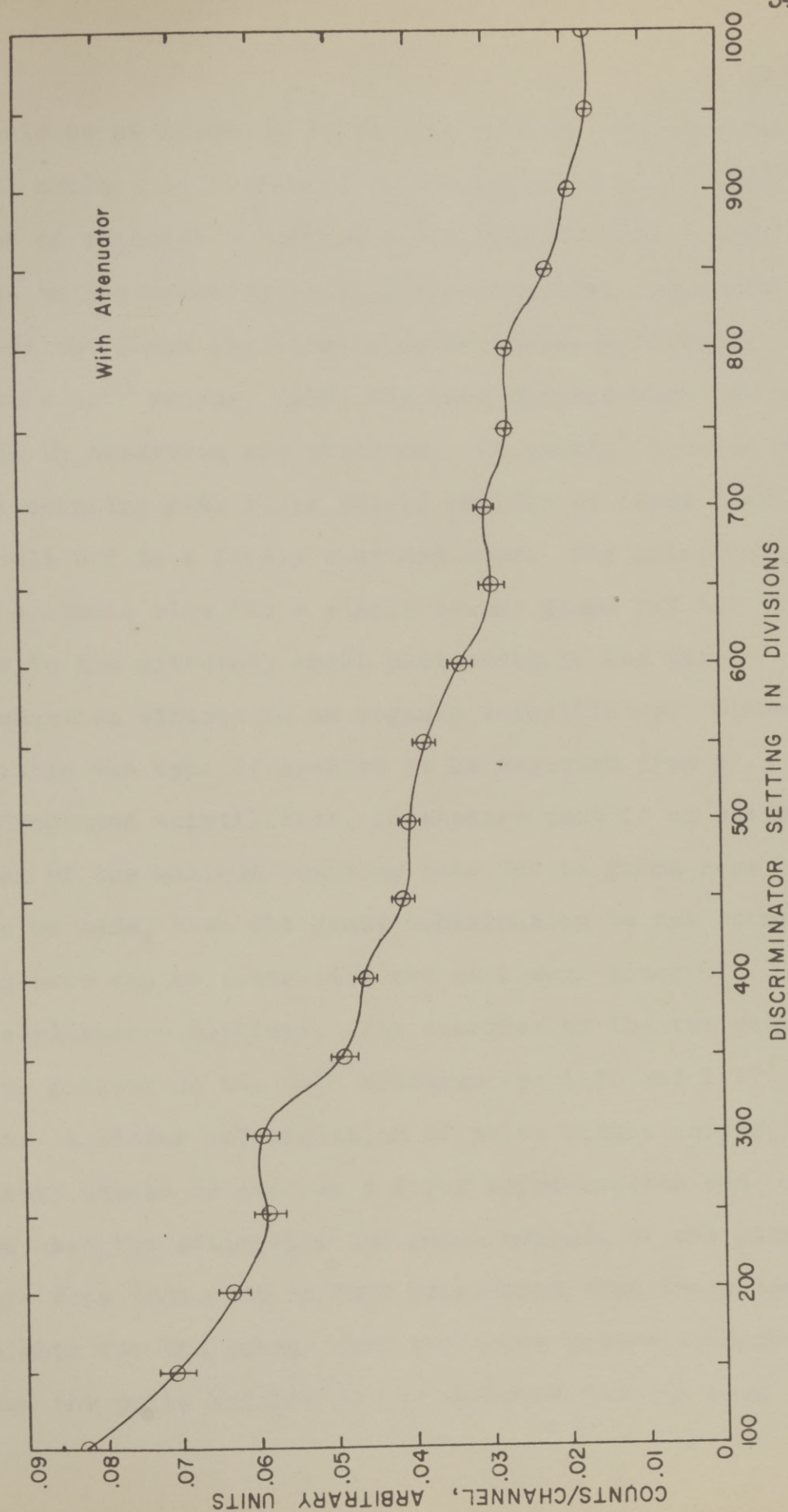


FIGURE 7. DISCRIMINATOR SPECTRUM OF SCATTERED NEUTRONS



should be at least one gamma ray emitted from the residual nucleus as it decays to the ground state. It is thus of interest to estimate the effect of the gamma rays on the counting rate of the detector. Figure 8 shows the gamma ray discriminator spectrum obtained from a  $\text{Co}^{60}$  source, using the same channel width as was used in observing the neutrons. It should be noted that the counting rate rises fairly rapidly at first then levels off to a fairly constant rate. The occurrence of a single rise for a single energy gamma ray is due to the extremely small photoelectric and pair production effects in an organic scintillator. Since this is the type of spectra to be expected from a hydrogenous scintillator, it appears that if an estimation of the maximum counting rate due to gamma rays can be made, then the gamma contribution to the counting rate can be subtracted out at lower values of discriminator settings. The energies of the two gamma rays present in the  $\text{Co}^{60}$  spectrum are 1.33 and 1.17 mev. A linear extrapolation of pulse height versus energy should be good as a first approximation and was used for estimating the pulse heights of the gamma rays from iron. It is very convenient that the pulse heights for the gammas turn out to be generally higher than the pulse heights of the neutrons for the same

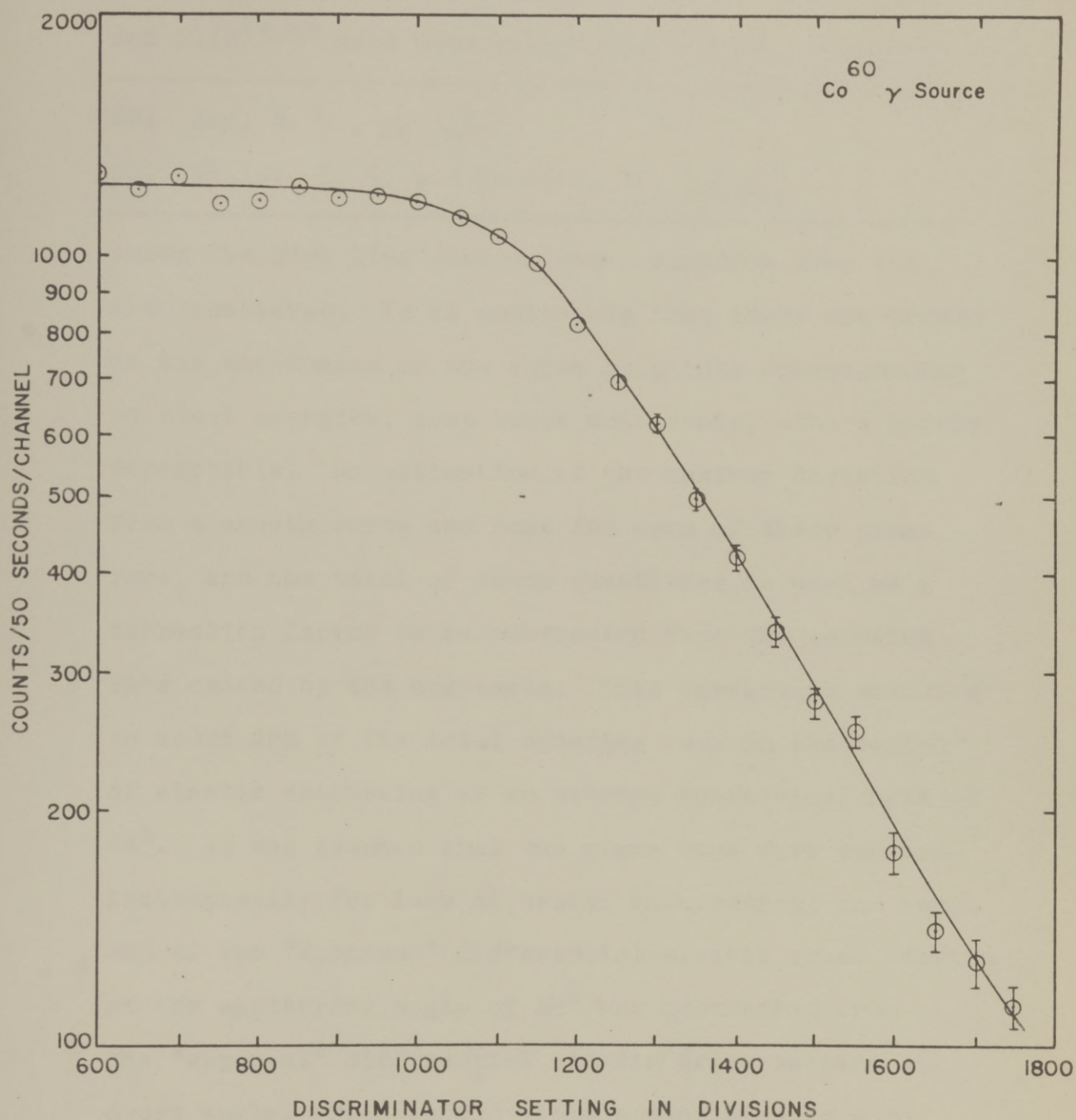


FIGURE 8. DISCRIMINATOR SPECTRUM OF  $^{60}\text{Co}$   $\gamma$  RAYS



energy.

Gamma rays of energies 0.845, 1.24, 1.42, 1.80 and 2.13<sup>22,23</sup> have been reported for iron. Figure 9

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22. Day, R. B., op cit.

23. Elliot, L. G. and Deutsch, M., op cit.

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shows the high bias discriminator spectrum from the iron scatterer. It is noticeable that there are breaks in the smoothness of the curve at points corresponding to these energies, some quite noticeable, others barely perceptible. An estimation of the maximum deviation from a smooth curve was made for each of these gamma rays, and the total of these quantities is used as a correction factor to be subtracted from the counting rate caused by the scatterer. This correction amounted to about 22% of the total counting rate in the region of elastic scattering at an average scattering angle of 44°. It was assumed that the gamma rays were emitted isotropically for lack of better information, and hence 22% of the "apparent" differential elastic cross section at the scattering angle of 44° was subtracted from the "apparent" differential elastic cross section at every angle. This should yield a considerably more accurate value of the differential elastic cross section. Since there were no gamma rays appearing in the

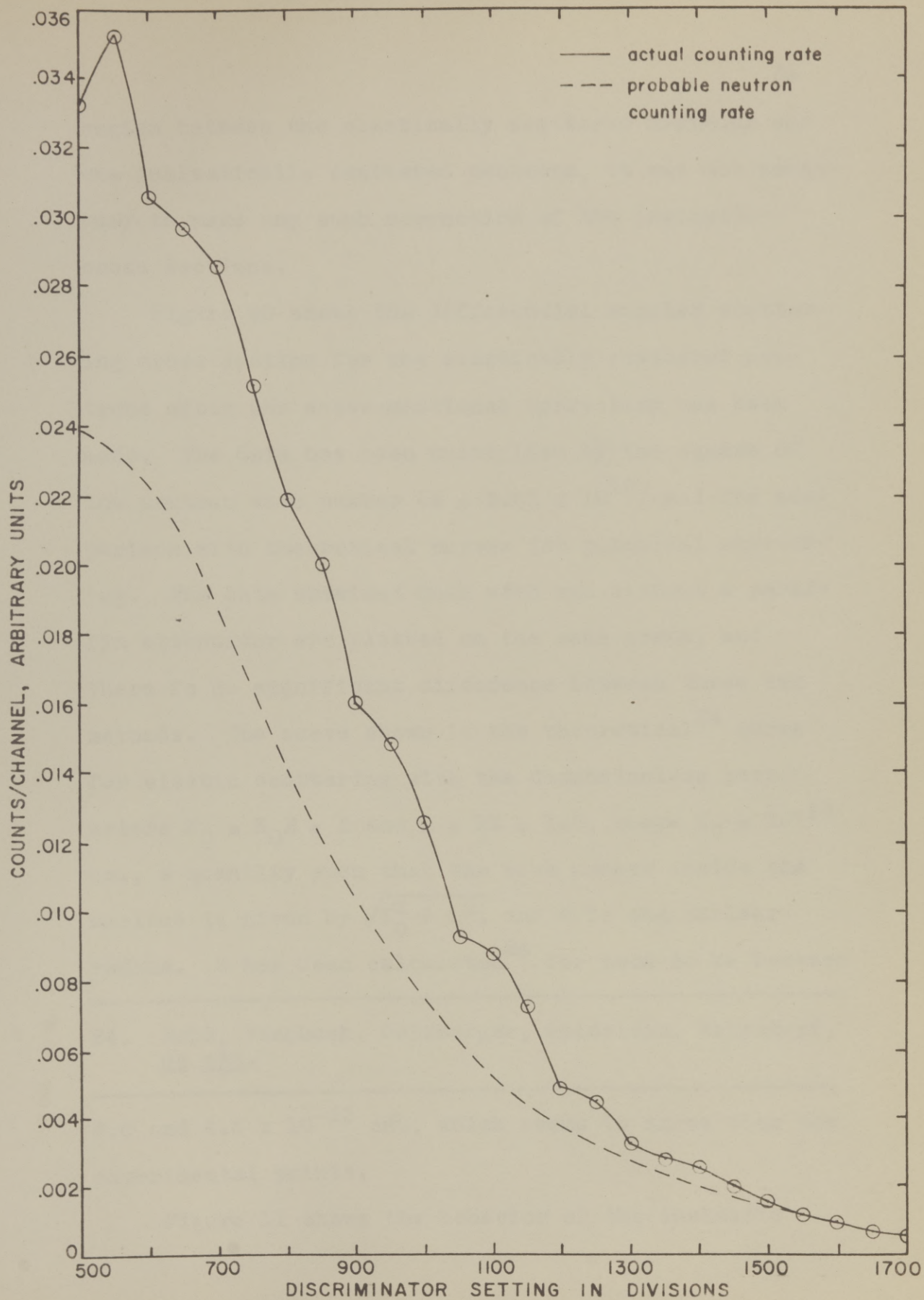


FIGURE 9. HIGH BIAS DISCRIMINATOR SPECTRUM OF SCATTERED NEUTRONS



region between the elastically scattered neutrons and the inelastically scattered neutrons, it was not necessary to make any such correction of the inelastic cross sections.

Figure 10 shows the differential angular scattering cross section for the elastically scattered neutrons after the above-mentioned correction has been made. The data has been multiplied by the square of the neutron wave number ( $k = 3.61 \times 10^{12}/\text{cm.}$ ) for comparison with theoretical curves for potential scattering. The data obtained both with and without a paraffin attenuator are plotted on the same graph, and there is no significant difference between these two methods. The curve shown is the theoretical<sup>24</sup> curve for elastic scattering with the dimensionless parameters  $X_0 = K_0 R = 5$  and  $x = kR = 1.7$ , where  $K_0 = 10^{-13}$  cm., a quantity such that the wave number inside the nucleus is given by  $\sqrt{K_0^2 + k^2}$ , and  $R$  is the nuclear radius.  $R$  has been calculated<sup>24</sup> for iron to be between

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24. Feld, Feshbach, Goldberger, Goldstein, Weisskopf, op cit.

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4.0 and  $4.6 \times 10^{-13}$  cm., which seems to agree with the experimental points.

Figure 11 shows the behavior of the inelastic

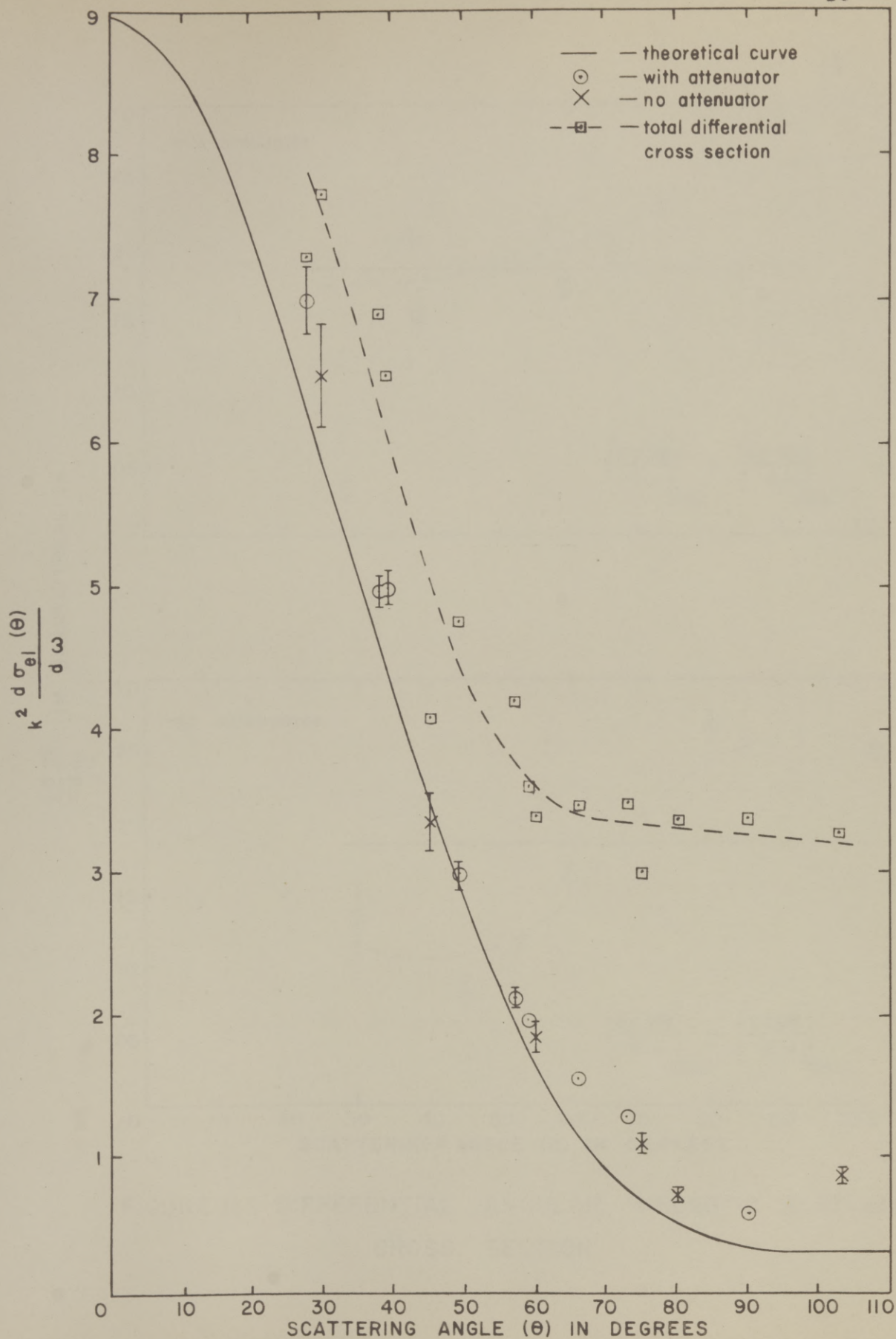


FIGURE 10. DIFFERENTIAL ANGULAR ELASTIC SCATTERING CROSS SECTION



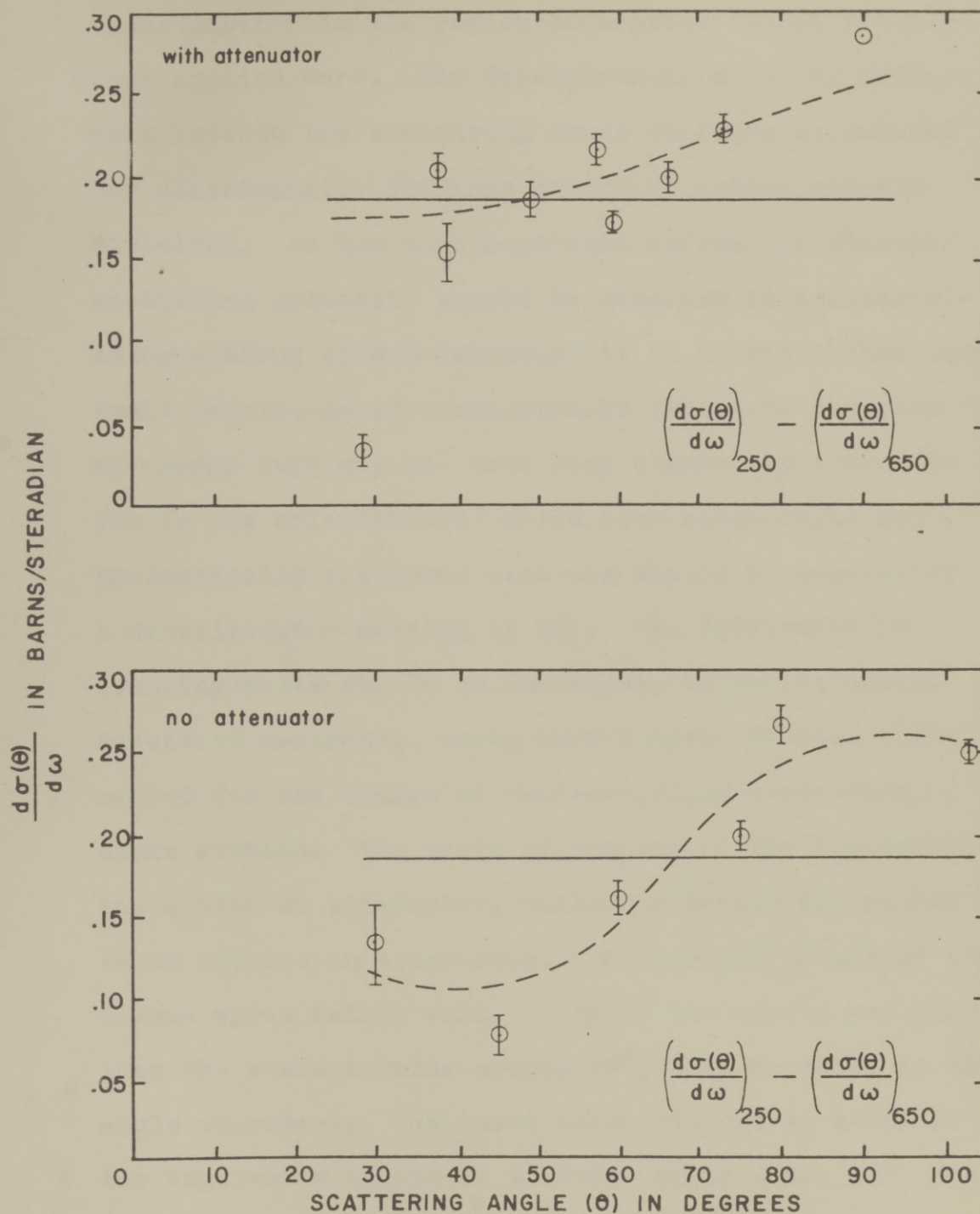


FIGURE II. DIFFERENTIAL ANGULAR INELASTIC SCATTERING CROSS SECTION

cross section in the region accessible to the techniques applied here. The data shown here is the difference between the scattering cross sections calculated for discriminator settings of 250 divisions and 650 divisions. As has been mentioned before the elastic scattering primarily should be observed at a discriminator setting of 650 (although it is possible that some small percentage of inelastically scattered neutrons and gamma rays may not have been completely corrected for in the calculations) while both elastically and inelastically scattered neutrons should be counted at a discriminator setting of 250. The difference in counting rates should be due solely to inelastically scattered neutrons. These curves have not been corrected for the change of neutron-proton scattering cross section. The curve at the top of the figure was taken with an attenuator, while the bottom figure was taken without an attenuator. The general shapes of the curves agree fairly well. Both of the curves are higher than the average value around  $90^\circ$ , then decrease as the angle decreases. The curve taken without an attenuator apparently begins to increase again after  $45^\circ$ , but it is difficult to tell whether the curve with the attenuator should do the same thing or not. A straight line has been drawn through the mean of the points of



both curves to indicate deviations from this mean. Dotted curves have been drawn to indicate the probable shape of the curves.

Figure 12 represents an attempt to subdivide the inelastic scattering into groups corresponding to the energy levels. This set of data was taken with an attenuator, but the statistics still leave considerable room for improvement. The best guess at the shape of an individual curve is probably a straight line. There is some evidence again of a consistent trend for the points at  $90^\circ$  to be higher than the average. Of course, trends which do not show up on the individual curves may show up on the composite curve which is plotted in Figure 11. Possibly counting times of the order of ten to one hundred times as long as the ones used or higher fluxes of neutrons might show up enough detail on these individual curves to warrant further conclusions to be drawn from them.

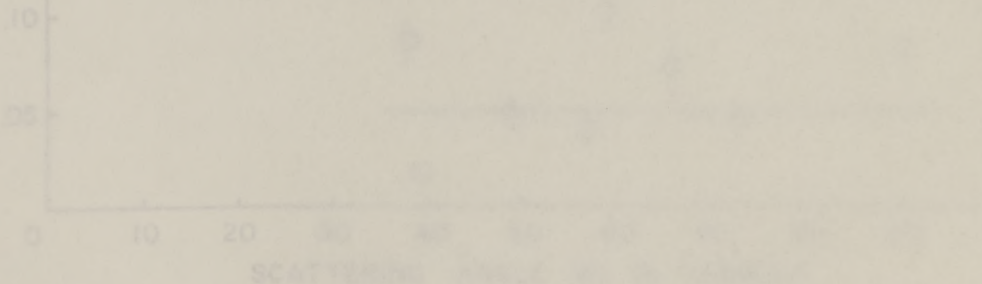


FIGURE 12. COMPONENTS OF INELASTIC SCATTERING BY  $^{238}\text{U}$

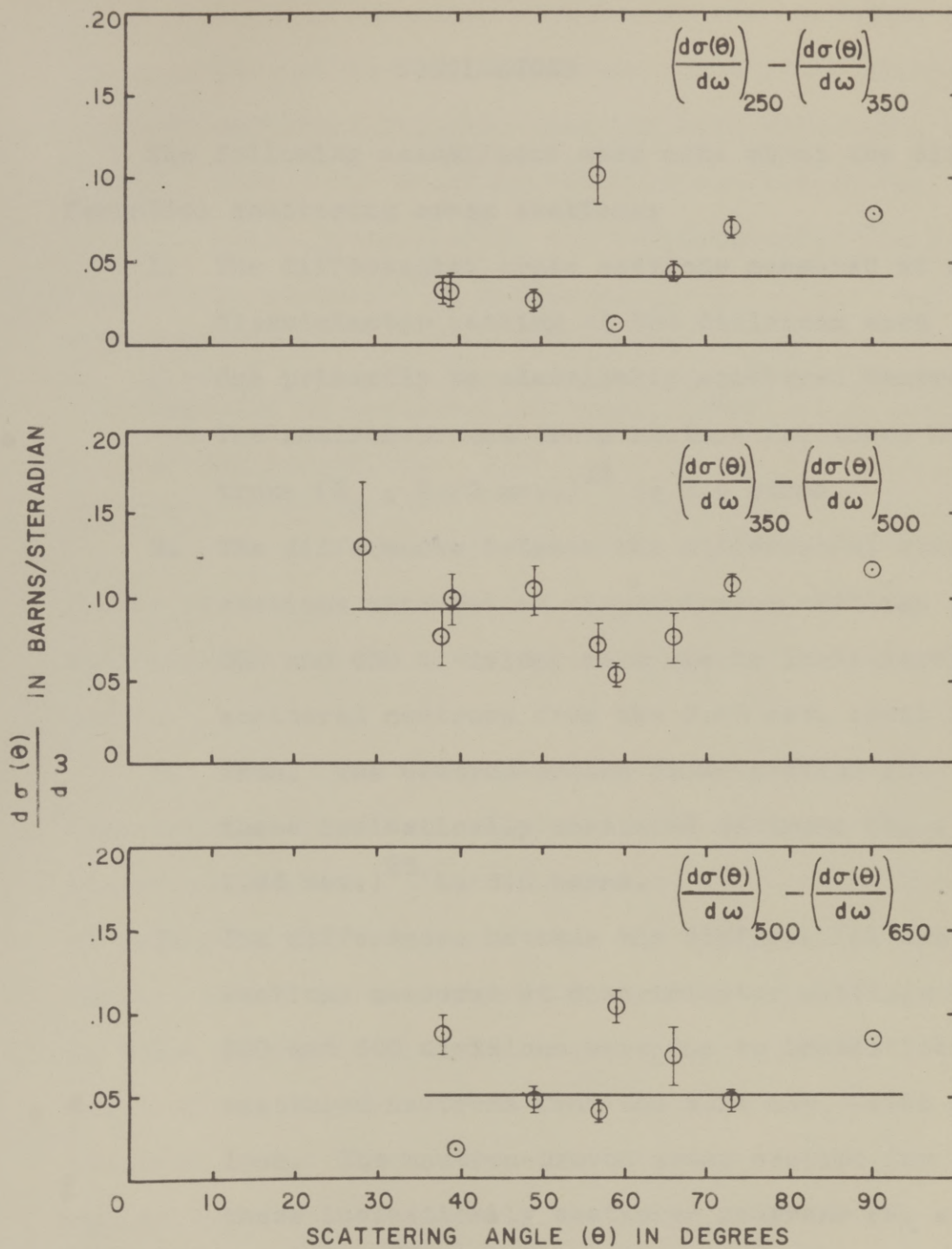


FIGURE 12. COMPONENTS OF DIFFERENTIAL ANGULAR INELASTIC SCATTERING CROSS SECTION



## CHAPTER VI

### CONCLUSIONS

The following assumptions were made about the differential scattering cross sections:

1. The differential cross sections measured at a discriminator setting of 650 divisions were due primarily to elastically scattered neutrons. The neutron-proton cross section for these neutrons ( $E_n = 2.80$  mev.)<sup>25</sup> is 2.4 barns.
2. The differences between the differential cross sections measured at discriminator settings of 500 and 650 divisions were due to inelastically scattered neutrons from the 0.85 mev. level of iron. The neutron-proton cross section for these inelastically scattered neutrons ( $E_n = 1.95$  mev.)<sup>25</sup> is 3.0 barns.
3. The differences between the differential cross sections measured at discriminator settings of 350 and 500 divisions were due to inelastically scattered neutrons from the 1.24 mev. level of iron. The neutron-proton cross section for these inelastically scattered neutrons ( $E_n = 1.56$  mev.)<sup>25</sup> is 3.3 barns.
4. The differences between the differential cross

and 2.6 sections measured at discriminator settings of value is 250 and 350 divisions were due to inelastically given by scattered neutrons from the 1.42 mev. level of iron. The neutron-proton cross section for these inelastically scattered neutrons ( $E_n = 1.38$  mev.)<sup>25</sup> is 3.5 barns.

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25. Allred, J. C. and Armstrong, A. H., "Laboratory Handbook of Nuclear Microscopy (Tentative)", Los Alamos Scientific Laboratory of the University of California, Nov. 1951.
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An average neutron-proton cross section correction factor of 0.74 is used on the curves for the total inelastically scattered neutrons, that is, the 250-650 curves.

The total inelastic scattering cross section is then calculated on the assumption of isotropy of the scattered neutrons. This calculation consists simply of multiplying the average value of the differential angular cross section, which is in barns/steradian, by  $4\pi$  which is the total solid angle about a point. A value of the inelastic cross section of 1.7 barns is obtained in this manner for the data taken both with and without the attenuator. The value of 1.7 barns agrees quite favorably with the values of Barschall and Ladenburg<sup>26</sup> which vary between the limits of 1.4

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26. Barschall and Ladenburg, op cit.
-



and 2.6 barns at a neutron energy of 2.5 mev. This value is somewhat higher than the value of 1.1 barns given by Barschall, et al.<sup>27</sup> from a "poor geometry"

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27. Barschall, Manley and Weisskopf, op cit.

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experiment at a neutron energy of 3.1 mev. An approximate integration of the elastic scattering yields a value of 1.6 barns for this cross section, which gives a total scattering cross section of 3.3 barns, which is in good agreement with the accepted value of 3.2 barns.<sup>28</sup>

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28. Miller, D. W., Adair, R. K., Bockelman, C. K., Dardes, S. F., Phy. Rev. 88, 83 (1952).

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It is somewhat difficult to estimate the probable error in the experiment. The averages of the experimental points for inelastic scattering with and without the attenuator are the same. The sum of the total elastic and the total inelastic cross sections differs by 3% from the accepted value of the total cross section. The assumption of slightly different functional forms for the angular variations of the cross sections may yield as much as  $\pm 5\%$  variation in the total cross section value. Small errors in measurements of distances may also contribute to the error. Considering

these various factors, it is believed that the error is not greater than  $\pm 10\%$  of the values measured.

Both graphs in Figure 11 indicate an anisotropy in the inelastic scattering. Unfortunately it was impossible to check the scattering at angles smaller than  $30^\circ$  and at angles larger than  $105^\circ$  with the scatterer used. Both the angular distributions measured are in fair agreement with an assumption of an angular distribution function of the form

$$\sigma(\theta) = A_0 + A_1 \cos^2 \theta$$

while the angular distribution measured without the discriminator, since this attenuator will tend to smear out the energy resolution of the counter. This distribution of the form

$$\sigma(\theta) = B_0 + B_1 \cos^2 \theta + B_2 \cos^4 \theta.$$

Either of these distribution functions might be expected from the predictions of Feld, et al.<sup>29</sup>

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29. Feld, Feshbach, Goldberger, Goldstein, Weisskopf, op cit.

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The method used here to obtain differential inelastic cross section has been shown to be feasible. The lower energy limit on the neutrons which can be measured is of the same order of magnitude as that of photographic plates. A slightly lower energy limit can be



CHAPTER VII

obtained with an ionization chamber although this limit is still about the same order of magnitude. The principal objection to ionization chambers and photographic plates is the length of time necessary to obtain data which is statistically reliable.

One factor which is present in the scintillation counter, which is not present in other methods, is the attenuation of light pulses originating in the scintillator volume farthest from the photocathode. This effect probably accounts for the absence of a very sharp break in the counting rate as a function of the discriminator, since this attenuation will tend to smear out the energy resolution of the counter. This difficulty could be evaded to some extent by making the scintillating volume thinner, although decreasing the volume will lower the efficiency of the counter. Some further improvement might also be gained by careful selection of the 5819 photomultiplier tubes for best linearity of pulse response to light pulses. It may be that scintillators other than terphenyl (such as anthracene) might give better resolution. The modifications given above coupled with longer counting time should improve the results to some extent, but the present results appear to be reliable.

# CHAPTER VII

## DATA TABLES

### SYMBOLS USED IN DATA TABLES

$d_1$  = distance from target to bottom of scatterer.

$d_2$  = distance from target to top of counter.

$d_3$  = distance from target to middle of scatterer.

$d_4$  = distance from target to middle of counter.

$R$  = distance from center of scatterer to center of counter.

$\theta$  = average scattering angle.

$E$  = position of discriminator dial.

$\Delta E$  = position of window width dial.

$I_0$  =  $\frac{\text{detector counts-background}}{\text{monitor counts-background}}$  with no scatterer present.

$\delta I$  = ratio of detector counts to monitor counts with scatterer in minus ratio of detector counts to monitor counts with scatterer out.





TABLE I (continued)

Time in Sec.	Div.	Scat- terer	Monitor Counts - Background	Detector Counts - Background	Detector-Background Monitor-Background	$\delta I$
300	550	In	69,987	37,690	.5385 $\pm$ .0023	
300	550	Out	70,310	34,394	.4892 $\pm$ .0022	.0493 $\pm$ .0033
300	600	In	71,263	38,221	.5363 $\pm$ .0023	
300	600	Out	68,055	33,571	.4933 $\pm$ .0022	.0430 $\pm$ .0033
300	650	In	71,755	37,164	.5179 $\pm$ .0022	
300	650	Out	71,042	34,113	.4802 $\pm$ .0022	.0377 $\pm$ .0031
300	700	In	71,717	35,562	.4959 $\pm$ .0022	
300	700	Out	64,022	29,466	.4602 $\pm$ .0022	.0357 $\pm$ .0031
300	800	In	69,414	31,318	.4512 $\pm$ .0021	
300	800	Out	65,078	26,944	.4140 $\pm$ .0020	.0372 $\pm$ .0030
300	900	In	71,477	28,534	.3992 $\pm$ .0019	
300	900	Out	64,721	24,045	.3715 $\pm$ .0019	.0277 $\pm$ .0027
300	1000	In	69,718	23,694	.3399 $\pm$ .0017	
300	1000	Out	67,003	20,705	.3090 $\pm$ .0017	.0309 $\pm$ .0024



TABLE II

Monitor Background = 1786/300 seconds

 $d_1 = 28.3 \text{ cm.}$  $d_4 = 31.0 \text{ cm.}$  $\Delta E = 556 = 50 \text{ Divisions of E}$  $d_2 = 28.1 \text{ cm.}$  $R^2 = 54.70 \text{ cm.}^2$ 

With Attenuator

 $d_3 = 26.5 \text{ cm.}$  $\theta = 65^\circ$ 

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	<u>Detector-Background</u> <u>Monitor-Background</u>	$\delta I$
300	50	In	13,439	3,666	.2728 $\pm$ .0034	.0400 $\pm$ .0014
300	50	Out	14,140	2,145	.1517 $\pm$ .0024	.1211 $\pm$ .0042
300	100	In	13,343	2,318	.1737 $\pm$ .0027	.0362 $\pm$ .0014
300	100	Out	22,612	2,064	.0913 $\pm$ .0016	.0824 $\pm$ .0032
300	150	In	15,786	2,231	.1413 $\pm$ .0022	.0351 $\pm$ .0013
300	150	Out	28,937	2,044	.0706 $\pm$ .0011	.0707 $\pm$ .0025
300	200	In	18,937	2,353	.1243 $\pm$ .0019	.0296 $\pm$ .0012
300	200	Out	35,492	2,159	.0608 $\pm$ .0010	.0635 $\pm$ .0022
300	250	In	18,332	2,099	.1145 $\pm$ .0018	.0330 $\pm$ .0012
300	250	Out	41,202	2,310	.0561 $\pm$ .0009	.0584 $\pm$ .0021
300	300	In	21,169	2,325	.1098 $\pm$ .0017	.0274 $\pm$ .0011
300	300	Out	41,408	2,080	.0502 $\pm$ .0008	.0596 $\pm$ .0019
300	350	In	21,726	2,090	.0962 $\pm$ .0015	.0278 $\pm$ .0016
300	350	Out	40,233	1,906	.0474 $\pm$ .0008	.0488 $\pm$ .0017
300	400	In	22,319	2,045	.0916 $\pm$ .0015	.0268 $\pm$ .0016
300	400	Out	39,448	1,799	.0456 $\pm$ .0008	.0460 $\pm$ .0017

TABLE II (continued)

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta$
300	450	In	24,686	1,998	.0809 $\pm$ .0013	.0410 $\pm$ .0015
300	450	Out	39,633	1,580	.0399 $\pm$ .0007	
300	500	In	27,116	2,084	.0769 $\pm$ .0012	.0400 $\pm$ .0014
300	500	Out	39,643	1,464	.0369 $\pm$ .0007	
300	550	In	27,943	2,059	.0737 $\pm$ .0012	.0382 $\pm$ .0014
300	550	Out	38,683	1,375	.0355 $\pm$ .0007	
300	600	In	28,964	1,939	.0669 $\pm$ .0011	.0331 $\pm$ .0013
300	600	Out	38,115	1,290	.0338 $\pm$ .0007	
300	650	In	33,924	2,115	.0623 $\pm$ .0010	.0296 $\pm$ .0012
300	650	Out	38,323	1,255	.0327 $\pm$ .0007	
300	700	In	34,021	1,987	.0584 $\pm$ .0010	.0300 $\pm$ .0012
300	700	Out	37,900	1,078	.0284 $\pm$ .0006	
300	750	In	38,037	2,125	.0559 $\pm$ .0009	.0274 $\pm$ .0011
300	750	Out	37,994	1,083	.0285 $\pm$ .0006	
300	800	In	43,822	2,298	.0524 $\pm$ .0008	.0272 $\pm$ .0010
300	800	Out	38,525	972	.0252 $\pm$ .0006	
300	850	In	42,999	1,996	.0464 $\pm$ .0007	.0220 $\pm$ .0010
300	850	Out	37,533	911	.0244 $\pm$ .0006	



TABLE II (continued)

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$
300	900	In	42,840	1,810	.0423 $\pm$ .0007	.0187 $\pm$ .0010
300	900	Out	37,380	881	.0236 $\pm$ .0006	
300	950	In	43,035	1,603	.0372 $\pm$ .0005	.0168 $\pm$ .0008
300	950	Out	38,014	777	.0204 $\pm$ .0005	
300	1000	In	42,742	1,560	.0365 $\pm$ .0005	.0173 $\pm$ .0008
300	1000	Out	38,217	735	.0192 $\pm$ .0005	

TABLE III\*

$\text{Co}^{60}$  source--1 meter from counter

$\Delta E = 278 = 25$  divisions of E

\*Note: Table III was taken with an amplifier  
gain  $\frac{1}{2}$  as much as Tables I, II, V, and VI.

Time in Sec.	E in Divisions	Counts
50	200	1526 $\pm$ 26
50	225	1383 $\pm$ 25
50	250	1306 $\pm$ 24
50	275	1321 $\pm$ 25
50	300	1276 $\pm$ 24
50	325	1205 $\pm$ 23
50	350	1257 $\pm$ 24
50	375	1164 $\pm$ 23
50	400	1178 $\pm$ 23
50	425	1225 $\pm$ 24
50	450	1187 $\pm$ 23
50	475	1194 $\pm$ 24
50	500	1176 $\pm$ 23
50	525	1119 $\pm$ 23
50	550	1065 $\pm$ 22
50	575	982 $\pm$ 21
50	600	829 $\pm$ 19
50	625	700 $\pm$ 18



TABLE III (continued)

Time in Sec.		E in Divisions		Counts
50		650		620 $\pm$ 17
50		675		501 $\pm$ 15
50		700		421 $\pm$ 14
50		725		339 $\pm$ 12
50		750		277 $\pm$ 11
50		775		253 $\pm$ 11
50		800		179 $\pm$ 9
50		825		142 $\pm$ 8
50		850		128 $\pm$ 8
50		875		114 $\pm$ 7
50		900		96 $\pm$ 7
50		925		86 $\pm$ 6
50		950		78 $\pm$ 6
50		975		60 $\pm$ 5
50		1000		47 $\pm$ 5
50		1025		31 $\pm$ 4
50		1050		22 $\pm$ 3

$\Delta E = 278 = 25$  Divisions of E

With Attenuator

\* Note: Table IV was taken with an amplifier

gain  $\hat{h}$  as much

Time E Scat- Monitor Counts Detector-Background  
in Sec. Div. terer -Background

500 250 Bkg. In. Out

500 275 Bkg. In. Out

500 300 Bkg. In. Out

500 325 Bkg. In. Out

500 350 Bkg. In. Out

500 375 Bkg. In. Out

500 400 Bkg. In. Out

500 425 Bkg. In. Out

500 450 Bkg. In. Out

500 475 Bkg. In. Out

500 500 Bkg. In. Out

TABLE IV\*

 $\Delta E = 278 = 25$  Divisions of E $d_1 = 26.5$  cm.  $d_4 = 34.9$  cm.

With Attenuator

 $d_2 = 32.0$  cm.  $R^2 = 138.04$  cm.<sup>2</sup>

\* Note: Table IV was taken with an amplifier

 $d_3 = 24.7$  cm.  $\theta = 44^\circ$ gain  $\frac{1}{2}$  as much as Tables I, II, V, and VI.

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\Delta I$
500	250	Bkg.	2,876	201		
600	250	In	95,415	6,806	.07133	
900	250	Out	211,181	8,052	.03813	.03320 $\pm$ .00068
500	275	Bkg.	2,791	177		
600	275	In	127,806	9,181	.07184	
900	275	Out	188,948	6,906	.03655	.03529 $\pm$ .00064
500	300	Bkg.	2,709	152		
600	300	In	125,876	8,114	.06446	
900	300	Out	186,954	6,320	.03381	.03065 $\pm$ .00061
504	325	Bkg.	2,849	119		
600	325	In	123,622	7,557	.06113	
900	325	Out	183,523	5,756	.03136	.02977 $\pm$ .00060
500	350	Bkg.	2,851	128		
600	350	In	124,561	7,037	.05649	
905	350	Out	186,040	5,179	.02784	.02865 $\pm$ .00056



TABLE IV (continued)

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background	
					Monitor-Background	$\delta I$
500	375	Bkg.	2,753	144		
800	375	In	151,872	7,701	.05071	
1000	375	Out	196,618	5,012	.02549	.02522 $\pm$ .00050
500	400	Bkg.	2,953	132		
900	400	In	187,096	8,551	.04570	
1200	400	Out	239,902	5,710	.02380	.02190 $\pm$ .00040
500	425	Bkg.	2,907	101		
900	425	In	211,182	8,621	.04082	
1200	425	Out	284,052	5,910	.02081	.02001 $\pm$ .00038
500	450	Bkg.	2,885	100		
900	450	In	183,582	6,439	.03507	
1200	450	Out	240,028	4,575	.01904	.01603 $\pm$ .00037
500	475	Bkg.	2,889	100		
900	475	In	208,711	6,464	.03097	
1200	475	Out	272,750	4,402	.01614	.01483 $\pm$ .00032
500	500	Bkg.	2,887	62		
900	500	In	184,918	4,952	.02678	
1250	500	Out	262,462	3,710	.01414	.01264 $\pm$ .00031
500	525	Bkg.	3,019	80		
900	525	In	174,925	3,751	.02144	
1200	525	Out	233,794	2,838	.01214	.00930 $\pm$ .00030

TABLE IV (continued)

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\Delta I$
500	550	Bkg.	2,866	97		
1200	550	In	215,355	3,957	.01837	.00881 $\pm$ .00026
1200	550	Out	216,565	2,070	.00956	
500	575	Bkg.	2,923	83		
910	575	In	157,114	2,466	.01570	.00731 $\pm$ .00026
1200	575	Out	209,324	1,757	.00839	
1000	600	Bkg.	5,894	140		
900	600	In	148,354	1,806	.01217	.00490 $\pm$ .00024
1500	600	Out	239,218	1,739	.00727	
500	625	Bkg.	2,925	65		
900	625	In	165,800	1,713	.01033	.00456 $\pm$ .00021
1500	625	Out	268,202	1,547	.00577	
1000	650	Bkg.	5,844	145		
4200	650	In	715,977	5,625	.00786	.00340 $\pm$ .00012
4800	650	Out	815,309	3,636	.00446	
1000	675	Bkg.	5,836	142		
1400	675	In	242,674	1,698	.00700	.00288 $\pm$ .00016
1900	675	Out	320,741	1,321	.00412	
1000	700	Bkg.	5,786	142		
1500	700	In	257,455	1,566	.00608	.00265 $\pm$ .00015
2300	700	Out	397,682	1,363	.00343	



TABLE IV (continued)

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$
1000	725	Bkg.	5,653	98		
1600	725	In	287,964	1,517	.00527	
2400	725	Out	444,157	1,451	.00327	.00200 $\pm$ .00013
1000	750	Bkg.	5,619	103		
2100	750	In	370,533	1,481	.00399	
3200	750	Out	557,533	1,278	.00231	.00168 $\pm$ .00011
800	775	Bkg.	4,510	49		
5700	775	In	1,186,947	3,933	.00331	
6300	775	Out	1,278,612	2,683	.00211	.00120 $\pm$ .00005
1000	800	Bkg.	5,644	64		
6000	800	In	1,177,405	3,248	.00276	
6000	800	Out	1,172,129	1,970	.00169	.00107 $\pm$ .00005
1000	825	Bkg.	5,683	66		
3000	825	In	556,763	1,255	.00225	
3000	825	Out	565,724	852	.00151	.00074 $\pm$ .00007
1000	850	Bkg.	5,705	57		
3000	850	In	557,958	1,084	.00194	
3000	850	Out	572,559	732	.00128	.00067 $\pm$ .00007

TABLE V

Monitor Background = 1740/300 sec.

 $\Delta E = 525 = 50$  Divisions of E $d_1 = 25.0$  cm. $d_3 = 23.3$  cm.

With Attenuator

 $R^2 = 627.25$  cm.<sup>2</sup> $\theta = 28^\circ$  $d_2 = 44.7$  cm. $d_4 = 47.6$  cm.

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	$\frac{\text{Detector-Background}}{\text{Monitor-Background}}$	$\delta I$
400	250	In	78,154	4,225	.05406	.01458 $\pm$ .00075
400	350		78,154	3,372	.04315	.01379 $\pm$ .00065
600	650		91,537	2,618	.02860	.01191 $\pm$ .00048
600	500		91,537	3,053	.03335	.01112 $\pm$ .00053
500	250	Out	76,370	3,015	.03948	
500	350		76,370	2,242	.02936	
600	650		92,246	1,540	.01669	
600	500		92,246	2,051	.02223	
150	250	Out	23,181	4,569	.1971	
150	350	No	23,181	4,126	.1780	
200	650	Atten.	31,372	5,312	.1693	
200	500		31,372	5,567	.1775	



TABLE V (continued)

$R^2 = 230.53 \text{ cm.}^2$		$\theta = 38^\circ$		$d_2 = 34.4 \text{ cm.}$		$d_4 = 37.3 \text{ cm.}$	
Time in Sec.	E Div.	Scatterer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$	
800	250	In	129,961	10,553	.08120		
800	350		129,961	8,934	.06874		
800	650		128,360	6,127	.04773		
800	500		128,360	7,461	.05813		
800	250	Out	132,234	6,006	.04542		
800	350		132,234	4,871	.03684		
800	650		130,205	3,231	.02481		
800	500		130,205	3,902	.02997		
						$.03578 \pm .00067$	
						$.03190 \pm .00061$	
						$.02292 \pm .00051$	
						$.02816 \pm .00055$	

TABLE V (continued)

$R^2 = 199.68 \text{ cm.}^2$		$\theta = 39^\circ$		$d_2 = 33.2 \text{ cm.}$		$d_4 = 36.1 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$	
400	250	In	61,869	5,730	.09262		
400	350		61,869	4,670	.07548		
600	650		90,086	4,874	.05410		
600	500		90,086	5,573	.06186		
600	250	Out	89,329	4,615	.05166	.04096 $\pm$ .00133	
600	350		89,329	3,499	.03917	.03631 $\pm$ .00085	
700	650		109,886	2,880	.02621	.02789 $\pm$ .00061	
700	500		109,886	3,531	.03213	.02973 $\pm$ .00067	
150	250	Out	24,237	7,812	.3223		
150	350	No	24,237	7,315	.3018		
150	650	Atten.	23,330	6,804	.2916		
150	500		23,330	6,979	.2991		





TABLE V (continued)

$R^2 = 76.28 \text{ cm.}^2$		$\theta = 57^\circ$		$d_2 = 26.8 \text{ cm.}$		$d_4 = 29.7 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\Sigma I$	
300	250	In	47,294	6,615	.13987		
300	350		47,294	5,019	.10612		
300	650		47,555	3,452	.07259		
300	500		47,555	4,188	.08807		
500	250	Out	82,999	5,290	.06374	.07613 $\pm$ .00127	
500	350		82,999	4,167	.05021	.05591 $\pm$ .00114	
500	650		86,217	2,968	.03442	.03817 $\pm$ .00093	
500	500		86,217	3,631	.04211	.04596 $\pm$ .00107	
200	250	Out	33,565	14,484	.4345		
200	350	No	33,565	13,556	.4039		
200	650	Atten.	33,404	13,144	.3935		
200	500		33,404	13,681	.4096		



TABLE V (continued)

$R^2 = 70.09 \text{ cm.}^2$		$\theta = 59^\circ$		$d_2 = 26.3 \text{ cm.}$		$d_4 = 29.2 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	<u>Detector-Background</u> <u>Monitor-Background</u>	$\delta I$	
600	250	In	108,161	14,198	.13127		
600	350		108,161	12,428	.11490		
600	650		110,437	8,076	.07313		
600	500		110,437	10,108	.09800		
600	250	Out	112,345	6,709	.05972	.07155 $\pm$ .00090	
600	350		112,345	5,571	.04959	.06531 $\pm$ .00084	
600	650		113,986	4,000	.03509	.03804 $\pm$ .00067	
600	500		113,986	4,707	.04129	.05671 $\pm$ .00078	

TABLE V (continued)

$R^2 = 56.34 \text{ cm.}^2$		$\theta = 66^\circ$		$d_2 = 25.0 \text{ cm.}$		$d_4 = 27.9 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$	
300	250	In	50,778	7,729	.15221		
300	350		50,778	6,303	.12413		
300	650		52,093	4,083	.07838		
300	500		52,093	5,218	.10017		
400	250	Out	72,798	4,904	.06736		
400	350		72,798	3,911	.05372		
400	650		71,507	2,808	.03927		
400	500		71,507	3,220	.04503		
200	250	Out	39,615	18,917	.4775		
200	350	No	39,615	18,051	.4552		
200	650	Atten.	39,354	17,412	.4424		
200	500		39,354	17,924	.4554		



TABLE V (continued)

$R^2 = 47.34 \text{ cm}^2$		$\theta = 73^\circ$		$d_2 = 23.9 \text{ cm.}$		$d_4 = 26.8 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$	
300	250	In	55,863	9,428	.16877		
300	350		55,863	7,585	.13578		
300	650		54,236	4,469	.08240		
300	500		54,236	5,598	.10322		
400	250	Out	73,801	5,094	.06902	.09975 $\pm$ .00136	
400	350		73,801	4,166	.05645	.07933 $\pm$ .00119	
500	650		93,324	3,802	.04074	.04166 $\pm$ .00094	
500	500		93,324	4,549	.04874	.05448 $\pm$ .00105	
300	250	Out	53,817	27,417	.5094		
300	350	No	53,817	26,392	.4904		
300	650	Atten.	52,372	25,191	.4810		
300	500		52,372	25,973	.4959		

TABLE V (continued)

$R^2 = 37.03 \text{ cm}^2$		$\theta = 90^\circ$		$d_2 = 21.9 \text{ cm.}$		$d_4 = 24.8 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\Delta I$	
600	250	In	99,614	20,394	.20473	.12552 $\pm$ .00096 .09915 $\pm$ .00053 .03852 $\pm$ .00064 .06639 $\pm$ .00070	
600	350		99,614	16,423	.16486		
600	650		114,682	11,082	.09663		
600	500		114,682	14,288	.12459		
600	250	Out	108,667	8,607	.07921	.12552 $\pm$ .00096 .09915 $\pm$ .00053 .03852 $\pm$ .00064 .06639 $\pm$ .00070	
600	350		108,667	7,141	.06571		
600	650		105,767	5,088	.04811		
600	500		105,767	6,156	.05820		
200	250	Out	35,689	20,677	.5794	.12552 $\pm$ .00096 .09915 $\pm$ .00053 .03852 $\pm$ .00064 .06639 $\pm$ .00070	
200	350	No	35,689	20,261	.5677		
200	650	Atten.	35,253	20,014	.5677		
200	500		35,253	20,747	.5885		



TABLE VI

 $K_1 = 31.89 \times 10^{-24} \text{ cm}^2/\text{steradian}$ 

With Attenuator

$\theta$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{650}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{500}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{350}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{250}$
28°	.6211	.5531	.6839	.6531
38°	.4662	.5546	.6320	.6676
39°	.4673	.4857	.5879	.6210
49°	.3135	.3619	.4691	.4976
57°	.2675	.3094	.3817	.4832
59°	.2352	.3396	.3939	.4060
66°	.2040	.2795	.3570	.4029
73°	.1821	.2309	.3400	.4116
90°	.1308	.2175	.3367	.4176

TABLE VII

With Attenuator  $K_1 = 31.89 \times 10^{-24}$  cm./steradian

$\theta$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{250}$	$-\left(\frac{d\sigma(\theta)}{d\omega}\right)_{350}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{350}$	$-\left(\frac{d\sigma(\theta)}{d\omega}\right)_{500}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{500}$	$-\left(\frac{d\sigma(\theta)}{d\omega}\right)_{650}$
28°	-.0308 ± .0385		.1308 ± .0411		-.0680 ± .0850	
38°	.0347 ± .0082		.0783 ± .0171		.0884 ± .0129	
39°	.0331 ± .0113		.1022 ± .0157		.0184 ± .0028	
49°	.0285 ± .0068		.1072 ± .0130		.0484 ± .0089	
57°	.1015 ± .0143		.0723 ± .0159		.0419 ± .0076	
59°	.0121 ± .0024		.0543 ± .0073		.1044 ± .0098	
66°	.0459 ± .0062		.0775 ± .0149		.0755 ± .0199	
73°	.0716 ± .0064		.1091 ± .0070		.0488 ± .0054	
90°	.0809 ± .0034		.1192 ± .0032		.0867 ± .0030	



TABLE VII (continued)

$\theta$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{250} - \left(\frac{d\sigma(\theta)}{d\omega}\right)_{650}$	$\frac{d\sigma_{el}(\theta)}{d\omega}$	$k^2 \frac{d\sigma_{el}(\theta)}{d\omega}$
28°	.0320 ± .0110	.5352 ± .017	6.99 ± .23
38°	.2014 ± .0133	.3803 ± .008	4.96 ± .11
39°	.1537 ± .0174	.3814 ± .009	4.98 ± .12
49°	.1841 ± .0107	.2276 ± .006	2.97 ± .08
57°	.2157 ± .0089	.1616 ± .005	2.11 ± .07
59°	.1708 ± .0060	.1493 ± .003	1.95 ± .04
66°	.1989 ± .0080	.1181 ± .004	1.54 ± .05
73°	.2295 ± .0067	.0962 ± .003	1.26 ± .04
90°	.2868 ± .0037	.0449 ± .001	.59 ± .02

TABLE VIII

Monitor Background = 2240/400 sec.

Detector Background (250) = 275/400 sec.

$\Delta E = 556 = 50$  Divisions of E

Detector Background (650) = 112/400 sec.

No Attenuator

$d_1 = 23.7$  cm.

$d_3 = 22.0$  cm.

$R^2 = 518.81 \text{ cm}^2$

$\theta = 30^\circ$

$d_2 = 41.3$  cm.

$d_4 = 44.2$  cm.

Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\delta I$
1200	650	In	301,159	59,831	.19867	
1200	650	Out	298,509	54,881	.18385	.01482 $\pm$ .00078
1200	250	In	296,548	67,778	.22856	
1200	250	Out	297,735	61,921	.20797	.02059 $\pm$ .00082

$R^2 = 134.80 \text{ cm}^2$

$\theta = 45^\circ$

$d_2 = 29.3$  cm.

$d_4 = 32.2$  cm.

900	650	In	196,122	74,101	.37783	
900	650	Out	198,775	68,536	.34479	.03304 $\pm$ .00130
900	250	In	207,030	88,930	.42955	
900	250	Out	204,398	78,545	.38427	.04528 $\pm$ .00135





TABLE VIII (continued)

$R^2 = 42.65 \text{ cm.}^2$		$\theta = 80^\circ$		$d_2 = 21.9 \text{ cm.}$		$d_4 = 24.8 \text{ cm.}$	
Time in Sec.	E Div.	Scat- terer	Monitor Counts -Background	Detector Counts -Background	Detector-Background Monitor-Background	$\Delta I$	
900	650	In	217,651	132,237	.60756		
900	650	Out	210,542	120,029	.57010		
900	250	In	211,748	151,232	.71421		
900	250	Out	205,219	122,079	.59487		
$R^2 = 34.80 \text{ cm.}^2$		$\theta = 103^\circ$		$d_2 = 19.3 \text{ cm.}$		$d_4 = 22.2 \text{ cm.}$	
900	650	In	248,364	185,440	.74665		
900	650	Out	244,449	169,774	.69452		
900	250	In	241,920	211,176	.87292		
900	250	Out	237,463	171,799	.72348		



TABLE IX

$$K_2 = 26.71 \times 10^{-24} \text{ cm}^2/\text{steradian}$$

Without Attenuator

$\theta$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{650}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{250}$	$\left(\frac{d\sigma(\theta)}{d\omega}\right)_{250} - \left(\frac{d\sigma(\theta)}{d\omega}\right)_{650}$	$\frac{d\sigma_{el}(\theta)}{d\omega}$	$K_2 \frac{d\sigma_{el}(0)}{d\omega}$
30°	.5718	.7025	.1305 ± .0256	.495	6.46 ± .35
45°	.3328	.4092	.0764 ± .0117	.256	3.34 ± .19
60°	.2164	.3770	.1606 ± .0092	.140	1.82 ± .11
75°	.1590	.3577	.1987 ± .0074	.082	1.08 ± .07
80°	.1321	.4031	.2710 ± .0070	.055	.71 ± .04
103°	.1416	.3897	.2481 ± .0062	.065	.85 ± .06

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